Electrical Measurements & Instrumentation

4th Semester

Diploma in Electrical and Electronics Engineering

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MESUREMENT:->

- Measurement of a given quantity is essentially & act all results of comparison between the quantity (whose magnitude is unknow) & predetermined or predefined standards. Since two quantities are compared the result is expressed in numerical value.
- Measurement is the process by which one can convert physical parameter to numerical numbers.

METHODS OF MEASUREMENT:

1.Direct methods

2.Indirect methods

1.DIRECT METHODS:

•In this method the unknown quantity (called measurement) is directly compared against a standard.

•The result is compared as a numerical number and a unit.

•Current is measured by Ammeter.

2.INDIRECT METHODS:

•In this indirect method of measurement the quality to be measured is not directly but other parameter related.e.g : Sometimes power can be measured by VXI method instead of measuring by wattmeter.

ACCURACY:

- 1. In analytical chemistry, the term 'accuracy' is used in relation to a chemical measurement.
- 2. The International Vocabulary of Basic and General Terms in Metrology (VIM) defines accuracy of measurement as... "closeness of the agreement between the result of a measurement and a true value." The VIM reminds us that accuracy is a "qualitative concept" and that a true value is indeterminate by nature.
- 3. In theory, a true value is that value that would be obtained by a perfect measurement. Since there is no perfect measurement in analytical chemistry, we can never know the true value.

ERRORS : in analytical chemistry are classified as systematic (determinate) and random (indeterminate). The VIM definitions of error, systematic error, and random error follow:

- 1. Error the result of a measurement minus a true value of the measurand.
- 2. Systematic Error the mean that would result from an infinite number of measurements of the same measurand carried out under repeatability conditions, minus a true value of the measurand.
- 3. Random Error the result of a measurement minus the mean that would result from an infinite number of measurements of the same measurand carried out under repeatability

The measured value is described as being biased high or low when a systematic error is present and the calculated uncertainty of the measured value is sufficiently small to see a definite difference when a comparison of the measured value to the conventional true value is made. Some analysts prefer the term 'determinate' instead of systematic because it is more descriptive in stating that this type of error can be determined. A systematic error can be estimated, but it cannot be known with certainty because the true value cannot be known. Systematic errors can therefore be avoided, i.e., they are determinate. Sources of systematic errors include spectral interferences, chemical standards, volumetric ware, and analytical balances where an improper calibration or use will result in a systematic error, i.e., a dirty glass pipette will always deliver less than the intended volume of liquid and a chemical standard that has an assigned value that is different from the true value will always bias the measurements either high or low and so on. The possibilities seem to be endless.

Random errors are unavoidable. They are unavoidable due to the fact that every physical measurement has limitation, i.e., some uncertainty. Using the utmost of care, the analyst can only obtain a weight to the uncertainty of the balance or deliver a volume to the uncertainty of the glass pipette. For example, most fourplace analytical balances are accurate to \pm 0.0001 grams. Therefore, with care, an analyst can measure a 1.0000 gram weight (true value) to an accuracy of \pm 0.0001 grams where a value of 1.0001 to 0.999 grams would be within the random error of measurement. If the analyst touches the weight with their finger andobtains a weight of 1.0005 grams, the total error = 1.0005 -1.0000 = 0.0005 grams and the random and systematic errors could be estimated to be 0.0001 and 0.0004 grams respectively. Note that the systematic error could be as great as 0.0006 grams, taking into account the uncertainty of the measurement.

PRECISION: -

The term precision is used in describing the agreement of a set of results among themselves. Precision is usually expressed in terms of the deviation of a set of results from the arithmetic mean of the set .

The term precision differs because of the observational error.

The precision is used for finding the consistency or reproductivity of the measurement.

MEASURING INSTRUMENTS:

1.1 Definition of instruments

An instrument is a device in which we can determine the magnitude or value of the quantity to be measured. The measuring quantity can be voltage, current, power and energy etc. Generally, instruments are classified in to two categories.

- A. Absolute Instrument
- B. Secondary Instrument

Absolute instrument

An absolute instrument determines the magnitude of the quantity to be measured in terms of the instrument parameter. This instrument is really used, because each time the value of the measuring quantities varies. So we have to calculate the magnitude of the measuring quantity, analytically which is time consuming. These types of instruments are suitable for laboratory use. Example: Tangent galvanometer.

Secondary instrument

This instrument determines the value of the quantity to be measured directly. Generally, these instruments are calibrated by comparing with another standard secondary instrument.

Examples of such instruments are voltmeter, ammeter and wattmeter etc. Practically Secondary instruments are suitable for measurement.

Secondary instruments

a.Indicating instruments

- b. Recording
- c. Integrating
- d. Electromechanically

Indicating instrument

This instrument uses a dial and pointer to determine the value of measuring quantity. The pointer indication gives the magnitude of measuring quantity.

A. Recording instrument

This type of instruments records the magnitude of the quantity to be measured continuously over a specified period of time.

B Integrating instrument

This type of instrument gives the total amount of the quantity to be measured over a specified period of time.

Electromechanical indicating instrument

For satisfactory operation electromechanical indicating instrument, three forces are necessary.

They are

(a) Deflecting force

(b) Controlling force

(c)Damping force

A: Deflecting force

When there is no input signal to the instrument, the pointer will be at its zero position. To deflect the pointer from its zero position, a force is necessary which is known as deflecting force.

A system which produces the deflecting force is known as a deflecting system. Generally, a deflecting system converts an electrical signal to a mechanical force.

B: Controlling force

To make the measurement indicated by the pointer definite (constant) a force is necessary which will be acting in the opposite direction to the deflecting force. This force is known as controlling force. A system which produces this force is known as a controlled system. When the external signal to be measured by the instrument is removed, the pointer should return back to the zero position. This is EEI, Semester 4th, Diploma Engineering (Electrical & Electronics)

possibly due to the controlling force and the pointer will be indicating a steady value when the deflecting torque is equal to controlling torque.

Td=Tc

Spring control

Two springs are attached on either end of spindle (Fig. 1.5). The spindle is placed in jewelled bearing, so that the frictional force between the pivot and spindle will be minimum. Two springs are provided in opposite direction to compensate the temperature error. The spring is made of phosphorous bronze.

When a current is supply, the pointer deflects due to rotation of the spindle. While spindle is rotate, the spring attached with the spindle will oppose the movements of the pointer. The torque produced by the spring is directly proportional to the pointer deflection θ . $\theta \propto CT$

The deflecting torque produced Td proportional to 'l'. When d C TT = , the pointer will come to a steady position. Therefore $I \propto \theta$

Since, θ and I are directly proportional to the scale of such instrument which uses spring controlled is uniform

C: Damping force

The deflection torque and controlling torque produced by systems are electro mechanical. Due to inertia produced by this system, the pointer oscillates about it final steady position before coming to rest. The time required to take the measurement is more. To damp out the oscillation is quickly, a damping force is necessary. This force is produced by different systems.

- (a) Air friction damping
- (b) Fluid friction damping
- (c) Eddy current damping

Air friction damping

The piston is mechanically connected to a spindle through the connecting rod (Fig. 1.6). The pointer is fixed to the spindle moves over a calibrated dial. When the pointer oscillates in clockwise direction, the piston goes inside and the cylinder gets compressed. The air pushes the piston upwards and the pointer tends to move in anticlockwise direction. If the pointer oscillates in anticlockwise direction the piston moves away and the pressure of the air inside cylinder gets reduced. The external pressure is more than that of the internal pressure.

Therefore, the piston moves down wards. The pointer tends to move in clock wise direction

Eddy current damping

An aluminum circular disc is fixed to the spindle. This disc is made to move in the magnetic field produced by a permanent magnet. When the disc oscillates it cuts the magnetic flux produced by damping magnet. An emf is induced in the circular disc by faradays law. Eddy currents are established in the disc since it has several closed paths. By Lenz's law, the current carrying disc produced a force in a direction opposite to oscillating force. The damping force can be varied by varying the projection of the magnet over the circular disc .

Permanent Magnet Moving Coil (PMMC) instrument:

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When D.C. supply is given to the moving coil, D.C. current flows through it. When the current carrying coil is kept in the magnetic field, it experiences a force. This force produces a torque and the former rotates. The pointer is attached with the spindle. When the former rotates, the pointer moves over the calibrated scale. When the polarity is reversed a torque is produced in the opposite direction. The mechanical stopper does not allow the deflection in the opposite direction. Therefore the polarity should be maintained with PMMC instrument.

If A.C. is supplied, a reversing torque is produced. This cannot produce a continuous deflection. Therefore this instrument cannot be used in A.C.

Torque developed by PMMC Let d T =deflecting torque C T = controlling torque θ = angle of deflection K=spring constant b=width of the coil I=height of the coil or length of coil N=No. of turns I=current B=Flux density A=area of the coil

Advantages Torque/weight is high Power consumption is less Scale is uniform Damping is very effective Since operating field is very strong, the effect of stray field is negligible Range of instrument can be extended Disadvantages Use only for D.C. Cost is high Error is produced due to ageing effect of PMMC Friction and temperature error are present.

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The force produced in the coil is given by F = sin

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When 0°= 90
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For N turns, F = NBIL

Torque produced r d FT $\perp \times =$ distance

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Td=NBIL X b =BINA
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Td=BANI

 $\mathbf{T} \varpropto \mathbf{I}$

Advantages

1. Torque/weight is high Power consumption is less Scale is uniform .

2.Damping is very effective Since operating field is very strong, the effect of stray field is negligible Range of instrument can be extended.

Disadvantages

1.Use only for D.C.

2.Cost is high

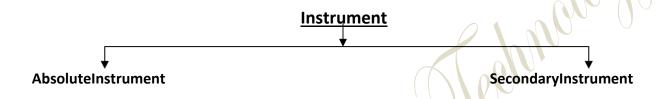
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MEASURING INSTRUMENTS

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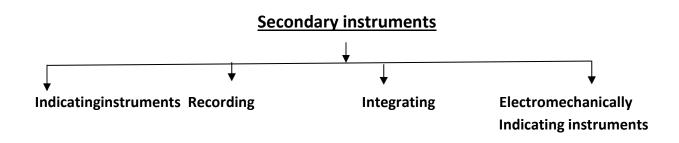
1.2 Absoluteinstrument

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1.4 Deflecting Force

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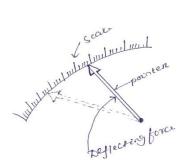
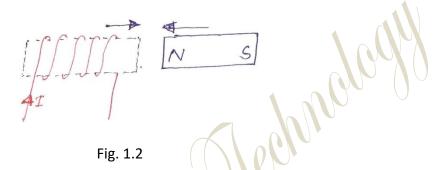


Fig. 1.1 Pointer scale

1.4.1 Magnitude Effect

When a current passes through the coil (Fig.1.2), it produces a imaginary bar magnet. When a soft-iron piece is brought near this coil it is magnetized. Depending upon the current direction the poles are produced in such a way that there will be a force of attraction between the coil and the soft iron piece. This principle is used in moving iron attraction typeinstrument.



If two soft iron pieces are place near a current carrying coil there will be a force of repulsion between the two soft iron pieces. This principle is utilized in the moving iron repulsion type instrument.

1.4.2 Force between a permanent magnet and a current carryingcoil

When a current carrying coil is placed under the influence of magnetic field produced by a permanent magnet and a force is produced between them. This principle is utilized in the moving coil type instrument.

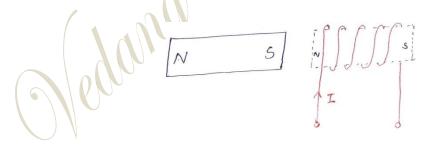


Fig. 1.3

1.4.3 Force between two current carryingcoil

When two current carrying coils are placed closer to each other there will be a force of repulsion between them. If one coil is movable and other is fixed, the movable coil will move away from the fixed one. This principle is utilized in electrodynamometer type instrument.

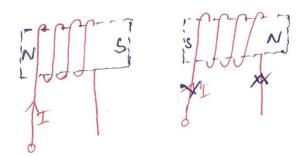


Fig. 1.4

1.5 Controllingforce

To make the measurement indicated by the pointer definite (constant) a force is necessary which will be acting in the opposite direction to the deflecting force. This force is known as controlling force. A system which produces this force is known as a controlled system. When the external signal to be measured by the instrument is removed, the pointer should return back to the zero position. This is possibly due to the controlling force and the pointer will be indicating a steady value when the deflecting torque is equal to controlling torque.

 $T_d = T_c$

(1.1)

1.5.1 Springcontrol

Two springs are attached on either end of spindle (Fig. 1.5). The spindle is placed in jewelled bearing, so that the frictional force between the pivot and spindle will be minimum. Two springs are provided in opposite direction to compensate the temperature error. The spring is made of phosphorous bronze.

When a current is supply, the pointer deflects due to rotation of the spindle. While spindle is rotate, the spring attached with the spindle will oppose the movements of the pointer. The torque produced by the spring is directly proportional to the pointer deflection θ .

$$T_C \propto \theta$$
 (1.2)

The deflecting torque produced T_d proportional to 'I'. When $T_C = T_d$, the pointer will come to a steady position. Therefore

 $\theta \infty I$

(1.3)

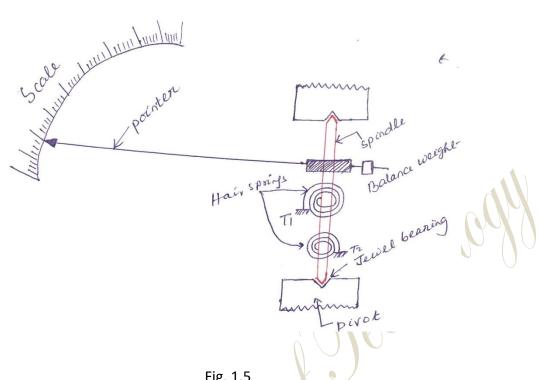


Fig. 1.5

Since, θ and I are directly proportional to the scale of such instrument which uses spring controlled is uniform.

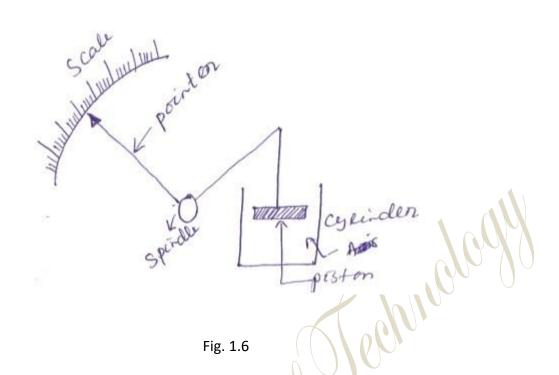
1.6 Damping Force

The deflection torque and controlling torque produced by systems are electro mechanical. Due to inertia produced by this system, the pointer oscillates about it final steady position before coming to rest. The time required to take the measurement is more. To damp out the oscillation is quickly, a damping force is necessary. This force is produced by differentsystems.

- (a) Air frictiondamping
- (b) Fluid frictiondamping
- (c) Eddy currentdamping

1.6.1 Air frictiondamping

The piston is mechanically connected to a spindle through the connecting rod (Fig. 1.6). The pointer is fixed to the spindle moves over a calibrated dial. When the pointer oscillates in clockwise direction, the piston goes inside and the cylinder gets compressed. The air pushes the piston upwards and the pointer tends to move in anticlockwise direction.



If the pointer oscillates in anticlockwise direction the piston moves away and the pressure of the air inside cylinder gets reduced. The external pressure is more than that of the internal pressure. Therefore the piston moves down wards. The pointer tends to move in clock wise direction.

1.6.2 Eddy currentdamping

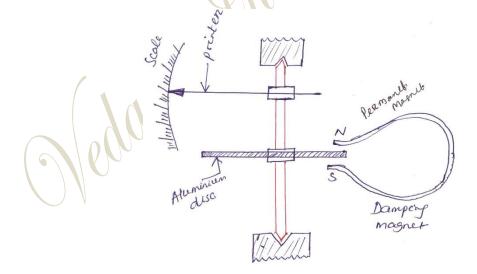
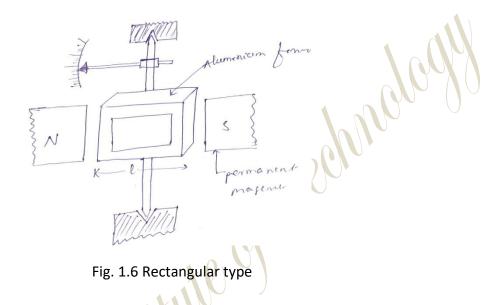


Fig. 1.6 Disc type

An aluminum circular disc is fixed to the spindle (Fig. 1.6). This disc is made to move in the magnetic field produced by a permanent magnet.

When the disc oscillates it cuts the magnetic flux produced by damping magnet. An emf is induced in the circular disc by faradays law. Eddy currents are established in the disc since it has several closed paths. By Lenz's law, the current carrying disc produced a force in a direction opposite to oscillating force. The damping force can be varied by varying the projection of the magnet over the circular disc.



1.7 Permanent Magnet Moving Coil (PMMC)instrument

One of the most accurate type of instrument used for D.C. measurements is PMMC instrument. **Construction:** A permanent magnet is used in this type instrument. Aluminum former is provided in the cylindrical in between two poles of the permanent magnet (Fig. 1.7). Coils are wound on the aluminum former which is connected with the spindle. This spindle is supported with jeweled bearing. Two springs are attached on either end of the spindle. The terminals of the moving coils are connected to the spring. Therefore the current flows through spring 1, moving coil and spring 2.

Damping: Eddy current damping is used. This is produced by aluminum former. Control: Spring control is used.

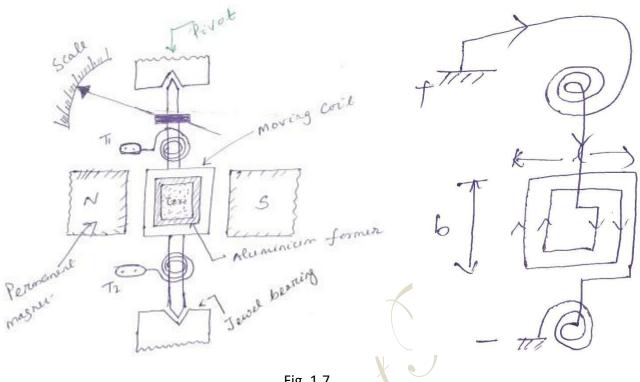


Fig. 1.7

Principle of operation

When D.C. supply is given to the moving coil, D.C. current flows through it. When the current carrying coil is kept in the magnetic field, it experiences a force. This force produces a torque and the former rotates. The pointer is attached with the spindle. When the former rotates, the pointer moves over the calibrated scale. When the polarity is reversed a torque is produced in the opposite direction. The mechanical stopper does not allow the deflection in the opposite direction. Therefore the polarity should be maintained with PMMCinstrument.

If A.C. is supplied, a reversing torque is produced. This cannot produce a continuous deflection. Therefore this instrument cannot be used in A.C.

Torque developed by PMMC

 T_d =deflecting torque Let T_C = controlling torque θ = angle of deflection K=spring constant b=width of the coil

I=height of the coil or length ofcoil N=No. ofturns I=current **B=Fluxdensity** A=area of the coil The force produced in the coil is given by (1.4) $F = BIL \sin \theta$ When $\theta = 90^{\circ}$ Mall For N turns, F = NBIL (1.5)(1.6)Torque produced $=F \times \perp_r$ distance $T_d = NBIL \times b = BINA$ (1.7) $T_d = BANI$ (1.8)tite $T_d \propto I$ (1.9)**Advantages** ✓ Torque/weight ishigh

- ✓ Power consumption isless
- ✓ Scale isuniform
- ✓ Damping is veryeffective
- ✓ Since operating field is very strong, the effect of stray field isnegligible
- ✓ Range of instrument can beextended

Disadvantages

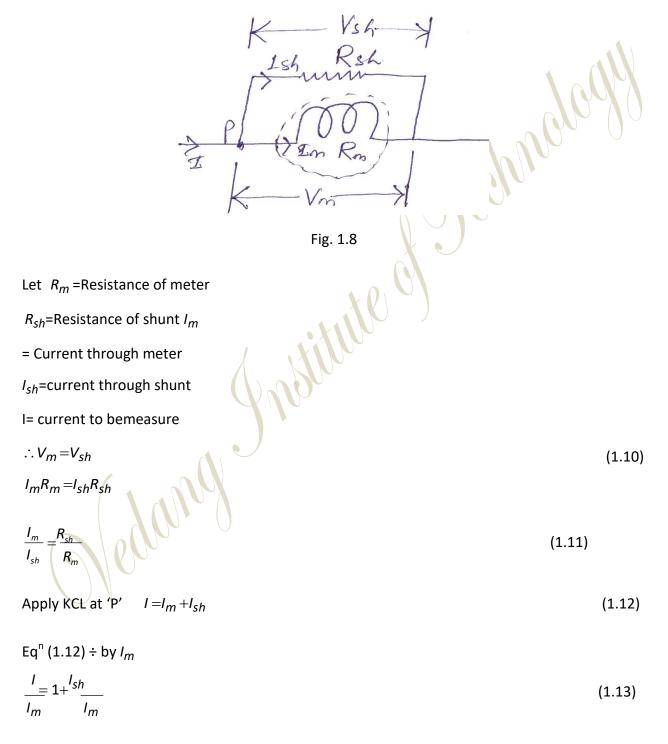
Td

- ✓ Use only forD.C.
- Cost ishigh
 - Error is produced due to ageing effect of PMMC
- ✓ Friction and temperature error are present

1.7.1 Extension of range of

PMMCinstrument Case-I:Shunt

A low shunt resistance connected in parrel with the ammeter to extent the range of current. Large current can be measured using low current rated ammeter by using a shunt.



$$\frac{I}{I_m} = 1 + \frac{R_m}{R_{sh}}$$

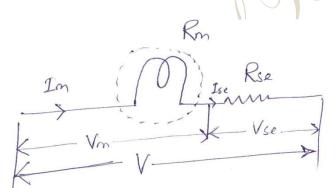
$$\therefore I = I_m \begin{pmatrix} R_m \\ 1 + \frac{R_m}{sh} \end{pmatrix}$$

$$\begin{pmatrix} 1 + \frac{R_m}{sh} \end{pmatrix}$$
 is called multiplication factor

Shunt resistance is made of manganin. This has least thermoelectric emf. The change is resistance, due to change in temperature is negligible.

Case (II): Multiplier

A large resistance is connected in series with voltmeter is called multiplier (Fig. 1.9). A large



voltage can be measured using a voltmeter of small rating with a multiplier.

Fig. 1.9

Let
$$R_m$$
 = resistance of meter

R_{se} = resistance of multiplier

 V_m =Voltage across meter

V_{se} = Voltage across seriesresistance

V= voltage to bemeasured

$$I_m = I_{se} \tag{1.16}$$

$$\frac{V_m}{R_m} = \frac{V_{se}}{R_{se}}$$
(1.17)

$$\therefore \frac{V_{se}}{V_m} = \frac{R_{se}}{R_m}$$
(1.18)

(1.14)

$$Apply KVL, V = V_m + V_{se} \tag{1.19}$$

$$\therefore V = V_m \begin{pmatrix} R_{se} \\ 1 + \frac{R_{m}}{m} \end{pmatrix}$$
(1.21)

$$\begin{pmatrix} R_{se} \\ 1 + \underline{R}_{m} \\ m \end{pmatrix} \rightarrow \text{Multiplication factor}$$

n

1.8 Moving Iron (MI)instruments

One of the most accurate instrument used for both AC and DC measurement is moving iron instrument. There are two types of moving iron instrument.

- Attractiontype
- Repulsiontype

1.8.1 Attraction type M.I.instrument

<u>Construction</u>: The moving iron fixed to the spindle is kept near the hollow fixed coil (Fig. 1.10). The pointer and balance weight are attached to the spindle, which is supported with jeweled bearing. Here air friction damping is used.

Principle of operation

The current to be measured is passed through the fixed coil. As the current is flow through the fixed coil, a magnetic field is produced. By magnetic induction the moving iron gets magnetized. The north pole of moving coil is attracted by the south pole of fixed coil. Thus the deflecting force is produced due to force of attraction. Since the moving iron is attached with the spindle, the spindle rotates and the pointer moves over the calibrated scale. But the force of attraction depends on the current flowing through the coil.

Torque developed by M.I

Let ' θ be the deflection corresponding to a current of 'i' amp Let the current increases by di, the corresponding deflection is ' θ + $d\theta$ '

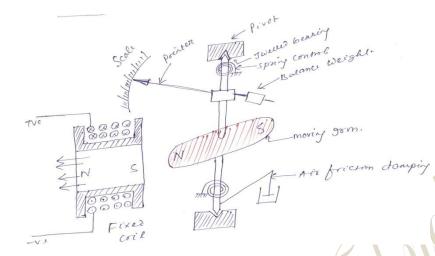


Fig. 1.10

There is change in inductance since the position of moving iron change w.r.t the fixed electromagnets.

Let the new inductance value be 'L+dL'. The current change by 'di' is dt seconds.

Let the emf induced in the coil be 'e' volt.

$$e = \frac{d}{dt} (Li) = L \frac{di}{dt} + \frac{dL}{dt}$$
(1.22)
Multiplying by 'idt' in equation (1.22)

$$e \times idt = L \frac{di}{dt} \times \frac{idt}{dt}$$
(1.23)

 $e \times idt = Lidi + i^2 dL$

Eqⁿ (1.24) gives the energy is used in to two forms. Part of energy is stored in the inductance. Remaining energy is converted in to mechanical energy which produces deflection.

000 Lfoll 10000 itdi

(1.24)

Fig. 1.11

Change in energy stored=Final energy-initial energy stored

$$\begin{aligned} &= \frac{1}{2}(L + dL)(i + di)^2 - \frac{1}{2}Lt^2 \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + di^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}\left\{(L + dL)(i^2 + 2idi) - Lt^2\right\} \\ &= \frac{1}{2}$$

When the instruments measure AC, $\theta \propto i^2 rms$

Scale of the instrument is non uniform.

Advantages

- ✓ MI can be used in AC and DC
- ✓ It ischeap
- ✓ Supply is given to a fixed coil, not in movingcoil.
- ✓ Simpleconstruction
- ✓ Less frictionerror.

Disadvantages

- ✓ It suffers from eddy current and hysteresiserror
- ✓ Scale is notuniform
- ✓ It consumed morepower
- ✓ Calibration is different for AC and DCoperation

1.8.2 <u>Repulsion type moving ironinstrument</u>

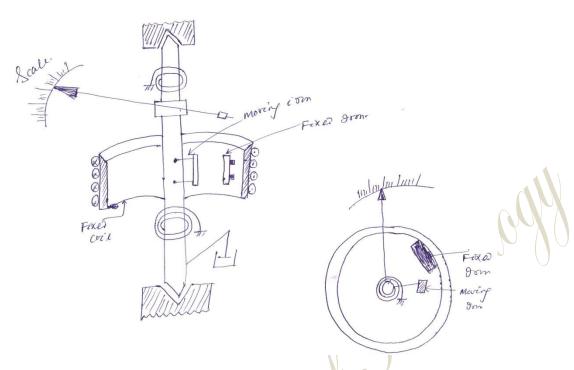
<u>Construction</u>: The repulsion type instrument has a hollow fixed iron attached to it (Fig. 1.12). The moving iron is connected to the spindle. The pointer is also attached to the spindle in supported with jeweled bearing.

huge

Principle of operation: When the current flows through the coil, a magnetic field is produced by it. So both fixed iron and moving iron are magnetized with the same polarity, since they are kept in the same magnetic field. Similar poles of fixed and moving iron get repelled. Thus the deflecting torque is produced due to magnetic repulsion. Since moving iron is attached to spindle, the spindle will move. So that pointer moves over the calibratedscale.

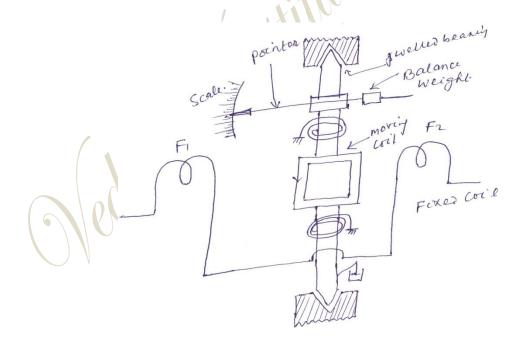
Damping: Air friction damping is used to reduce the oscillation.

Control: Spring control is used.





1.9 Dynamometer (or) Electromagnetic moving coil instrument(EMMC)





This instrument can be used for the measurement of voltage, current and power. The difference between the PMMC and dynamometer type instrument is that the permanent magnet is replaced by an electromagnet.

Construction: A fixed coil is divided in to two equal half. The moving coil is placed between the two half of the fixed coil. Both the fixed and moving coils are air cored. So that the hysteresis effect will be zero. The pointer is attached with the spindle. In a non metallic former the moving coil is wounded.

Control: Spring control is used.

Damping: Air friction damping is used.

Principle of operation:

When the current flows through the fixed coil, it produced a magnetic field, whose flux density is proportional to the current through the fixed coil. The moving coil is kept in between the fixed coil. When the current passes through the moving coil, a magnetic field is produced by this coil.

The magnetic poles are produced in such a way that the torque produced on the moving coil deflects the pointer over the calibrated scale. This instrument works on AC and DC. When AC voltage is applied, alternating current flows through the fixed coil and moving coil. When the current in the fixed coil reverses, the current in the moving coil also reverses. Torque remains in the same direction. Since the current i_1 and i_2 reverse simultaneously. This is because the fixed and moving coils are either connected in series or parallel.

<u>Torque developed by EMMC</u>

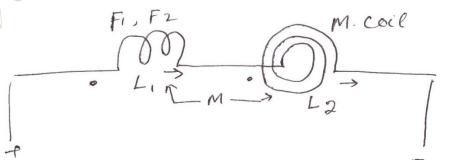


Fig. 1.14

Let

L₁=Self inductance of fixed coil L₂=

Self inductance of moving coil

M=mutual inductance between fixed coil and moving coil

i₁₌current through fixed coil

i₂=current through moving coil

Total inductance of system,

$$L_{total} = L_1 + L_2 + 2M$$

But we know that in case of M.I

$$L_{total} = L_1 + L_2 + 2M$$
But we know that in case of M.I
$$T_d = \frac{1}{2} i^2 \frac{d(L)}{d\theta}$$

$$T_d = \frac{1}{2} i^2 \frac{d}{d\theta} (L_1 + L_2 + 2M)$$
(1.33)
(1.34)
(1.35)

The value of L₁ and L₂ are independent of ' θ ' but 'M' varies with θ

$$T = \frac{1}{d} i^{2} \times 2 \frac{dM}{d\theta}$$

$$T_{d} = i^{2} \frac{dM}{d\theta}$$
(1.36)
(1.37)

If the coils are not connected in series $i_1 \neq i_2$

$$\therefore T_d = i_1 i_2 \frac{dM}{d\theta}$$
(1.38)

$$T_C = T_d \tag{1.39}$$

$$\therefore \theta = \frac{i_1 i_2 dM}{K d\theta}$$
(1.40)

Hence the deflection of pointer is proportional to the current passing through fixed coil and moving coil.

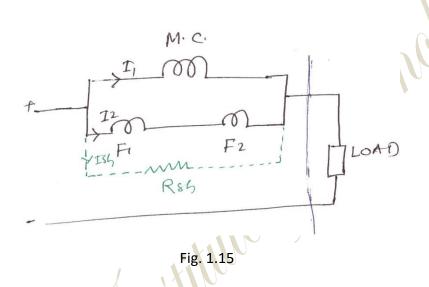
1.9.1 Extension of

EMMCinstrument Case-I

Ammeterconnection

Fixed coil and moving coil are connected in parallel for ammeter connection. The coils are designed such that the resistance of each branch is same.

Therefore



To extend the range of current a shunt may be connected in parallel with the meter. The value R_{sh} is designed such that equal current flows through moving coil and fixed coil.

$$\therefore T_d = I_1 I_2 \frac{dM}{d6} \tag{1.41}$$

$$\text{Or} : T_d = I^2 \frac{dM}{d\theta}$$
(1.42)

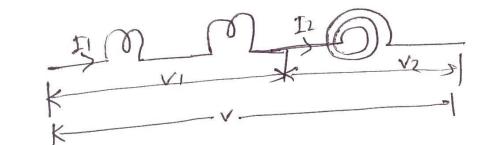
$$T_C = K\theta \tag{1.43}$$

$$\theta = \frac{I^2 dM}{K d\theta} \tag{1.44}$$

$$\therefore \theta \propto I^2 \text{ (Scale is not uniform)}$$
(1.45)

Case-II Voltmeter connection

Fixed coil and moving coil are connected in series for voltmeter connection. A multiplier may be connected in series to extent the range of voltmeter.



$$I = \frac{V_1}{Z_1} I_2 = \frac{V_2}{Z_2}$$
(1.46)

$$T_d = \frac{V_1}{Z_1} \times \frac{V_2}{Z_2} \times \frac{dM}{d\theta}$$
(1.47)

$$T_d = \frac{K_1 V}{Z_1} \times \frac{K_2 V}{Z_2} \times \frac{dM}{d\theta}$$
(1.48)

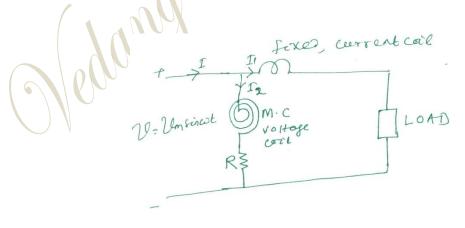
$$T_d = \frac{KV^2}{Z_1 Z_2} \times \frac{dM}{d\theta}$$
(1.49)

$$T_d \propto V^2 \tag{1.50}$$

$$\therefore \theta \propto V^2$$
 (Scale in not uniform) (1.51)

Case-III As wattmeter

When the two coils are connected to parallel, the instrument can be used as a wattmeter. Fixed coil is connected in series with the load. Moving coil is connected in parallel with the load. The moving coil is known as voltage coil or pressure coil and fixed coil is known as current coil.





Assume that the supply voltage is sinusoidal. If the impedance of the coil is neglected in comparison with the resistance 'R'. The current,

$$I_2 = \frac{v_m \sin wt}{R} \tag{1.52}$$

Let the phase difference between the currents I_1 and I_2 is ϕ

$$I_1 = I_m \sin(wt - \phi) \tag{1.53}$$

$$T_d = I_1 I_2 \frac{dM}{d\theta} \tag{1.54}$$

$$T_{d} = I_{m} \sin(wt - \phi) \times \frac{V_{m} \sin wt \, dM}{R \, d\theta}$$
(1.55)

$$T = \frac{1}{(IV\sin wt\sin(wt - \phi))} \frac{dM}{d\theta}$$
(1.56)

$$T = \frac{1}{I} V \sin wt . \sin(wt - \phi) \frac{dM}{d\theta}$$
(1.57)

The average deflecting torque

$$(T_d)_{avg} = \frac{1}{2\Pi} \int_0^{2\Pi} T_d \stackrel{\times}{}^d (mt)$$
(1.58)

$$(T_d)_{avg} = \frac{1}{2\Pi} \int_0^{2\Pi} \frac{1}{R} \times I_m \sin wt. \sin(wt - \phi) \quad \frac{dM}{d\theta} \times d^{(wt)}$$
(1.59)

$$(T_{d})_{wg} = \frac{VI}{2 \times 2\Pi} \times \frac{1}{R} \times \frac{dM}{d\theta} \left[\int \{\cos\phi - \cos(2wt - \phi)\} dwt \right]$$
(1.60)

$$(T^{d})^{avg} = \frac{\underline{K}_{\Pi}}{mm} \times \frac{d\mathcal{M}}{mm} \begin{bmatrix} 2 \frac{1}{2} \Pi & 2 \frac{1}{2} \Pi \\ \cos \phi . dwt - \cos(2wt - \phi) . dwt \end{bmatrix}$$
(1.61)

$$(T_{d avg}) = \frac{V_m I_m}{4\Pi R} \times \frac{dM}{d\theta} \left[\cos \phi [wt]^{2\Pi} \right]$$
(1.62)

$$(T_{davg}) = \frac{V_m I_m}{4\Pi R} \times \frac{dM}{d\theta} \left[\cos\phi(2\Pi - 0) \right]$$
(1.63)

$$(T_{davg}) = \frac{V_m I_m}{2} \times \frac{1}{R} \times \frac{dM}{d\theta} \times \cos\phi$$
(1.64)

$$(T_d)_{avg} = V_{rms} \times I_{rms} \times \cos\phi \times \frac{1}{R} \times \frac{dM}{d\theta}$$
(1.65)

 $(T_d)_{avg} \propto KVI \cos \phi$

 $T_C \propto \theta$

 $\theta \propto KVI \cos \phi$

 $\theta \propto V I \cos \phi$

Errors in PMMC

- ✓ The permanent magnet produced error due to ageing effect. By heat treatment, this error can beeliminated.
- The spring produces error due to ageing effect. By heat treating the spring the error can beeliminated.
- ✓ When the temperature changes, the resistance of the coil vary and the spring also produces error in deflection. This error can be minimized by using a spring whose temperature co-efficient is verylow.

1.10 Difference between attraction and repulsion typeinstrument

An attraction type instrument will usually have a lower inductance, compare to repulsion type instrument. But in other hand, repulsion type instruments are more suitable for economical production in manufacture and nearly uniform scale is more easily obtained. They are therefore much more common than attraction type.

Repaired

1.11 Characteristics of meter

1.11.1 Full scale deflection current(*I_{FSD}*)

The current required to bring the pointer to full-scale or extreme right side of the instrument is called full scale deflection current. It must be as small as possible. Typical value is between 2 μ A to 30mA.

1.11.2 **Resistance of the coil(***R_m***)**

This is ohmic resistance of the moving coil. It is due to ρ , L and A. For an ammeter this should be as small as possible.

1.11.3 Sensitivity of themeter(S)

$$S = \frac{1}{I_{FSD}} (\Omega / volt), \uparrow S = \frac{Z \uparrow}{V}$$

It is also called ohms/volt rating of the instrument. Larger the sensitivity of an instrument, more accurate is the instrument. It is measured in Ω /volt. When the sensitivity is high, the impedance of meter is high. Hence it draws less current and loading affect is negligible. It is also defend as one over full scale deflectioncurrent.

1.12 Error in M.linstrument

1.12.1 Temperature error

Due to temperature variation, the resistance of the coil varies. This affects the deflection of the instrument. The coil should be made of manganin, so that the resistance is almost constant.

1.12.2 Hysteresiserror

Due to hysteresis affect the reading of the instrument will not be correct. When the current is decreasing, the flux produced will not decrease suddenly. Due to this the meter reads a higher value of current. Similarly when the current increases the meter reads a lower value of current. This produces error in deflection. This error can be eliminated using small iron parts with narrow hysteresis loop so that the demagnetization takes place very quickly.

1.12.3 Eddy currenterror

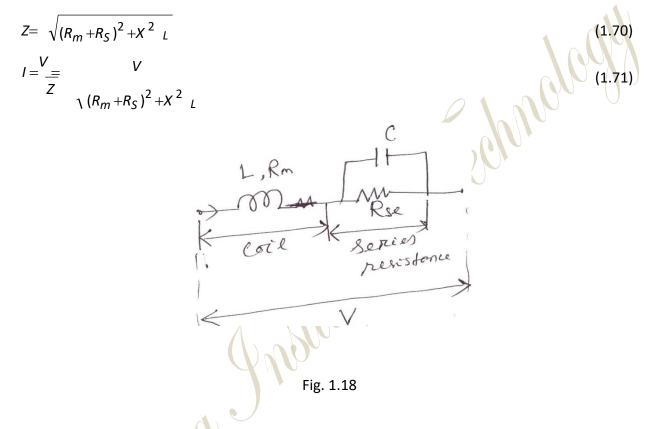
The eddy currents induced in the moving iron affect the deflection. This error can be reduced by increasing the resistance of the iron.

1.12.4 Stray fielderror

Since the operating field is weak, the effect of stray field is more. Due to this, error is produced in deflection. This can be eliminated by shielding the parts of theinstrument.

1.12.5 Frequencyerror

When the frequency changes the reactance of the coil changes.



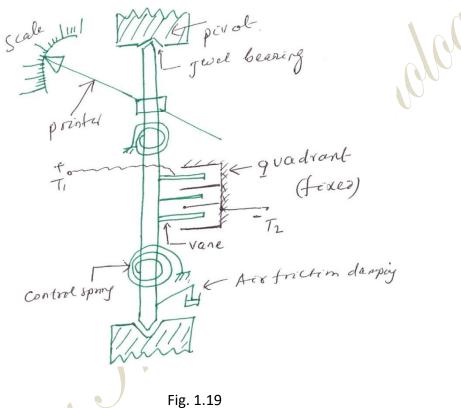
Deflection of moving iron voltmeter depends upon the current through the coil. Therefore, deflection for a given voltage will be less at higher frequency than at low frequency. A capacitor is connected in parallel with multiplier resistance. The net reactance, ($x_L - x_C$) is very small, when compared to the series resistance. Thus the circuit impedance is made independent of frequency. This is because of the circuit is almost resistive.

$$C = 0.41 \frac{L}{\left(R_{\rm S}\right)^2} \tag{1.72}$$

1.13 Electrostatic Instrument

In multi cellular construction several vans and quadrants are provided. The voltage is to be measured is applied between the vanes and quadrant. The force of attraction between the vanes and quadrant produces a deflecting torque. Controlling torque is produced by spring control. Air friction damping is used.

The instrument is generally used for measuring medium and high voltage. The voltage is reduced to low value by using capacitor potential divider. The force of attraction is proportional to the square of the voltage.



Torque develop by electrostatic

instrument V=Voltage applied between vane

and quadrant C=capacitance between vane

and guadrant

Energy stored =
$$\frac{1}{2}CV^2$$

(1.73)

Let ' θ be the deflection corresponding to a voltage V.

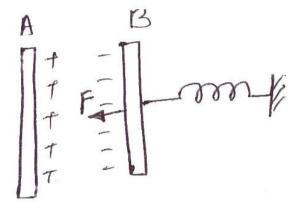
Let the voltage increases by dv, the corresponding deflection is $\theta + d\theta$

When the voltage is being increased, a capacitive current flows

 $i = \frac{dq}{dt} = \frac{d(CV)}{dt} = \frac{dC}{dt}V + C\frac{dV}{dt}$

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 $V \times dt$ multiply on both side of equation (1.74)







$$Vidt = \frac{dC}{dt}V^2dt + CV\frac{dV}{dt}dt$$
(1.75)

$$Vidt = V^2 dC + CV dV \tag{1.76}$$

Change in stored energy=
$$\frac{1}{2}(C+dC)(V+dV)^2 - \frac{1}{2}CV^2$$
 (1.77)

$$= \frac{1}{2} \left[(C+dC)V^{2} + dV^{2} + 2VdV \right] - \frac{1}{2}CV^{2}$$

$$= \frac{1}{2} \left[CV^{2} + CdV^{2} + 2CVdV + V^{2}dC + dCdV^{2} + 2VdVdC \right] - \frac{1}{2}CV^{2}$$

$$= \frac{1}{2}V^{2}dC + CVdV$$

$$V^{2}dC + CVdV = \frac{1}{2}V^{2}dC + CVdV + F \times rd\theta$$
(1.78)

$$T_{d} \times d\theta = \frac{1}{2} \frac{V^2}{2} dC \tag{1.79}$$

$$T = \frac{1}{2} \frac{V^2 \left(\frac{dC}{d\theta}\right)}{\left(\frac{d\theta}{d\theta}\right)}$$
(1.80)

At steady state condition, $T_d = T_C$

$$K\theta = \frac{1}{V} \frac{V^{2} \left(\frac{dC}{d\theta} \right)}{2 \left(\frac{d\theta}{d\theta} \right)}$$

$$\theta = \frac{1}{V} \frac{V^{2} \left(\frac{dC}{d\theta} \right)}{2K \left(\frac{d\theta}{d\theta} \right)}$$
(1.81)
(1.82)

Advantages

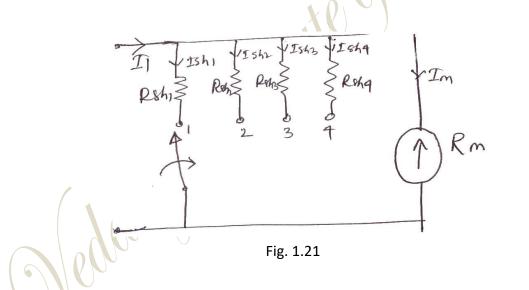
- ✓ It is used in both AC and DC.
- ✓ There is no frequencyerror.
- ✓ There is no hysteresiserror.
- ✓ There is no stray magnetic field error. Because the instrument works on electrostatic principle.
- ✓ It is used for highvoltage
- ✓ Power consumption isnegligible.

Disadvantages

- ✓ Scale is notuniform
- ✓ Large insize
- ✓ Cost ismore

1.14 Multi rangeAmmeter

When the switch is connected to position (1), the supplied current I_1

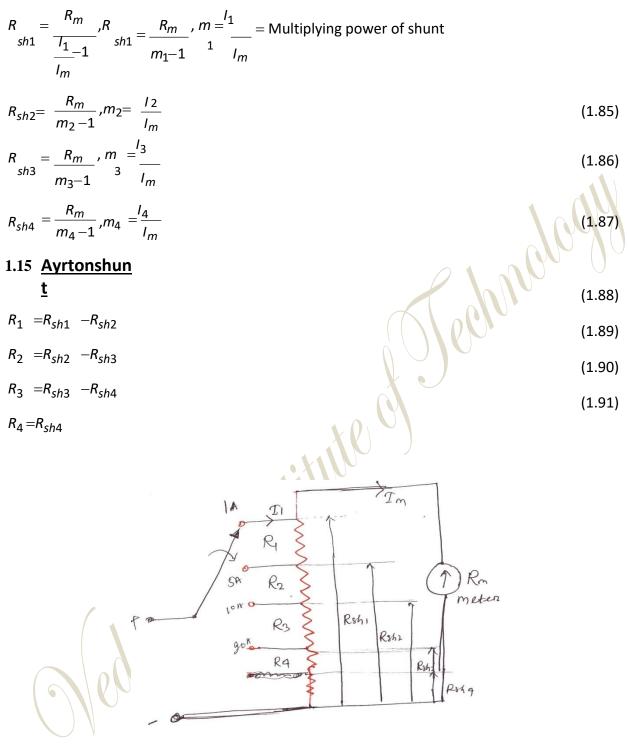


$$I_{sh1}R_{sh1} = I_m R_m$$

 $R_{sh1} = \frac{I_m R_m}{I_{sh1}} = \frac{I_m R_m}{I_1 - I_m}$ (1.84)

(1.83)

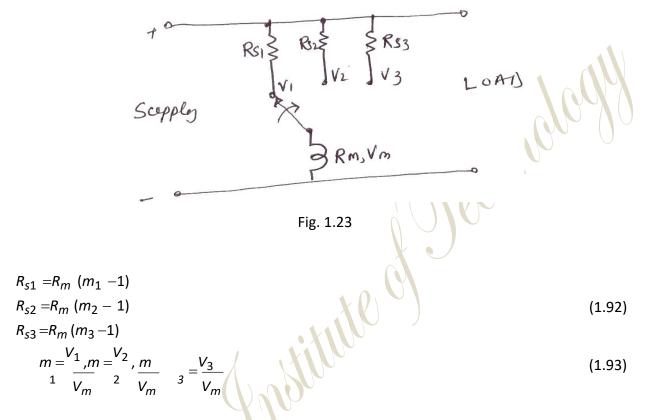
hmalad





Ayrton shunt is also called universal shunt. Ayrton shunt has more sections of resistance. Taps are brought out from various points of the resistor. The variable points in the o/p can be connected to any position. Various meters require different types of shunts. The Aryton shunt is used in the lab, so that any value of resistance between minimum and maximum specified can be used. It eliminates the possibility of having the meter in the circuit without a shunt.

1.16 Multi range D.C.voltmeter



We can obtain different Voltage ranges by connecting different value of multiplier resistor in series with the meter. The number of these resistors is equal to the number of ranges required.

1.17 Potential dividerarrangement

The R_1, R_2, R_3 and R_4 is connected in series to obtained the ranges V_1, V_2, V_3 and V_4 resistance

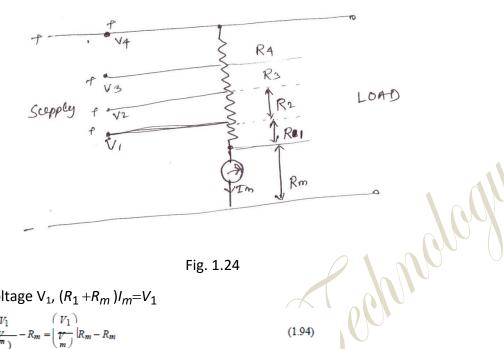


Fig. 1.24

(1.94)

(1.95)

(1.98) (1.99)

Consider for voltage V₁, $(R_1 + R_m)I_m = V_1$

$$\therefore R_1 = \frac{V_1}{m} - R_m = \frac{V_1}{\binom{m}{r}} - R_m = \binom{V_1}{\binom{m}{r}} R_m$$

$$R_1 = (m_1 - 1)R_m$$

For V₂,
$$(R_2 + R_1 + R_m)I_m = V_2 \Longrightarrow R_2 = \frac{V_2}{I_m} - R_1 - R_m$$
 (1.96)

$$R_{2} = \frac{V_{2}}{\binom{V}{V}} - (m_{1} - 1)R_{m} - R_{m}$$
(1.97)

$$R_2 = m_2 R_m - R_m - (m_1 - 1) R_m$$

$$= R_m (m_2 - 1 - m_1 + 1)$$

$$R_2 = (m_2 - m_1)R_m$$

For $V_3(R_3 + R_2 + R_1 + R_m)I_m = V_3$ $R = \frac{V_3}{R_2 - R_2 - R_1 - R_2}$

$$= \frac{V_3}{V_m} \frac{R_1 - R_2 - R_1 - R_m}{m}$$

= $\frac{V_3}{V_m} \frac{R_m}{m} - \frac{(m_2 - m_1)R_m}{m} - \frac{(m_1 - 1)R_m}{m} - \frac{R_m}{m}$
= $m_3 R_m - (m_2 - m_1)R_m - (m_1 - 1)R_m - R_m$
 $R_3 = (m_3 - m_2)R_m$

For V₄
$$(R_4 + R_3 + R_2 + R_1 + R_m)I_m = V_4$$

 $R_4 = \frac{V_4}{I_m} - R_3 - R_2 - R_1 - R_m$
 $= \begin{pmatrix} V_4 \\ \frac{V}{m} \end{pmatrix} R_m - (m_3 - m_2)R_m - (m_2 - m_1)R_m - (m_1 - 1)R_m - R_m$
 $R_4 = R_m [m_4 - m_3 + m_2 - m_2 + m_1 - m_1 + 1 - 1]$
 $R_4 = (m_4 - m_3)R_m$

Example: 1.1

A PMMC ammeter has the following specification

Coil dimension are 1cm×1cm. Spring constant is 0.15×10^{-6} N -m / rad Flux density is

 1.5×10^{-3} wb/ m². Determine the no. of turns required to produce a deflection of 90⁰ when a current 2mA flows through the coil.

puele

Solution:

```
At steady state condition T_d = T_C

BANI = K\theta

\Rightarrow N = \frac{K\theta}{BAI}

A=1\times10^{-4} m^2

K= 0.15 \times 10^{-6} \frac{N-m}{rad}

B=1.5 \times 10^{-3} wb/m^2

I= 2 \times 10^{-3} A

\theta = 90^\circ = \frac{\Pi}{2} rad

N=785 ans.
```

Example;: 1.2

The pointer of a moving coil instrument gives full scale deflection of 20mA. The potential difference across the meter when carrying 20mA is 400mV. The instrument to be used is 200A for full scale deflection. Find the shunt resistance required to achieve this, if the instrument to be used as a voltmeter for full scale reading with 1000V. Find the series resistance to be connected it?

Solution

```
Case-1

V_m = 400 \text{mV}

I_m = 20 mA

I = 200 \text{A}

R_m = \frac{V_m}{I_m} = \frac{400}{20} = 20 \Omega

I = I_m \left(1 + \frac{R_m}{R_{sh}}\right)

200 = 20 \times 10^{-3} \left[1 + \frac{20}{R_{sh}}\right]

R_{sh} = 2 \times 10^{-3} \Omega
```

Case-II
V=1000V

$$V = V_m \left(1 + \frac{R_{se}}{m} \right)$$

$$4000 = 400 \times 10^{-3} \left(1 + \frac{R_{se}}{20} \right)$$

$$R_{se} = 49.98 k\Omega$$

Example: 1.3

A 150 v moving iron voltmeter is intended for 50HZ, has a resistance of $3k\Omega$. Find the series resistance required to extent the range of instrument to 300v. If the 300V instrument is used to measure a d.c. voltage of 200V. Find the voltage across the meter?

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Solution:

$$R_m = 3k\Omega$$
, $V_m = 150V$, $V = 300V$

$$V = V_m \begin{pmatrix} R_{se} \\ 1 + \frac{R_{se}}{m} \end{pmatrix}$$

$$300 = \begin{pmatrix} + R_{se} \\ 150 \\ 1 \\ \frac{-1}{3} \end{pmatrix} \Rightarrow R = 3k\Omega$$

Case-II $V = V_m \begin{pmatrix} R_{se} \\ 1 + \frac{R_{se}}{m} \end{pmatrix}$

$$200 = V_m \begin{pmatrix} 1 + \frac{3}{3} \\ 3 \end{pmatrix}$$

$$\therefore V_m = 100V \text{ Ans}$$

Example: 1,4

What is the value of series resistance to be used to extent '0' to 200V range of 20,000 Ω /volt voltmeter to 0 to 2000 volt?

Solution:

 $V_{se} = V - V = 1800$

$$I_{FSD} = \frac{1}{20000} = \frac{\Box 1}{Sensitivity}$$

 $V_{se} = R_{se} \times i_{FSD} \Longrightarrow R_{se} = 36M\Omega$

Example: 1.5

A moving coil instrument whose resistance is 25Ω gives a full scale deflection with a current of 1mA. This instrument is to be used with a manganin shunt, to extent its range to 100mA. Calculate the error caused by a 10^{0} C rise in temperature when:

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- (a) Copper moving coil is connected directly across the manganinshunt.
- (b) A75ohmmanganinresistanceisusedinserieswiththeinstrumentmovingcoil. The temperature co-efficient of copper is $0.004/^{0}$ C and that of manganin is $0.00015^{0}/$ C. Solution:

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Case-1

 $I_m = 1mA$

 $R_m = 25\Omega$

I=100mA

$$I = I_m \begin{pmatrix} R_m \\ 1 + \frac{R_m}{sh} \end{pmatrix}$$
$$100 = 1 \begin{pmatrix} 25 \\ 1 + \frac{25}{sh} \end{pmatrix} \Rightarrow \frac{25}{R_m} = 99$$
$$\Rightarrow R_{sh} = \frac{25}{99} = 0.2525\Omega$$

Instrument resistance for 10[°]C rise in temperature,

 $R_{mt} = 25(1 + 0.004 \times 10)$

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 $R_t = R_o (1 + \rho_t \times t)$ $R_{m/t=10}^{\circ} = 26\Omega$

Shunt resistance for 10[°]C, rise in temperature

$$R_{sh/t=10}^{\circ} = 0.2525(1 + 0.00015 \times 10) = 0.2529\Omega$$

Current through the meter for 100mA in the main circuit for 10⁰C rise in temperature

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$$I = I_m \left(1 + \frac{R_m}{R_{sh}} \right) | t = 10°C$$

$$100 = I_{mt} \left(1 + \frac{26}{0.2529} \right)$$

$$I_m |_{t=10} = 0.963 mA$$

But normal meter current=1mA

Error due to rise in temperature=(0.963-1)*100=-3.7%

Case-b As voltmeter

Total resistance in the meter circuit= $R_m + R_{sh} = 25 + 75 = 100\Omega$

$$I = I_m \begin{pmatrix} R_m \\ 1 + \frac{R_m}{sh} \end{pmatrix}$$
$$100 = 1 \begin{pmatrix} 100 \\ 1 + \frac{R_m}{sh} \end{pmatrix}$$
$$R_{sh} = \frac{100}{100 \pm} = 1.01\Omega$$

Resistance of the instrument circuit for 10⁰C rise in temperature

 $R_{m|_{t=10}} = 25(1 + 0.004 \times 10) + 75(1 + 0.00015 \times 10) = 101.11\Omega$

Shunt resistance for 10[°]C rise in temperature

 $R_{m|_{t=10}} = 25(1 + 0.004 \times 10) + 75(1 + 0.00015 \times 10)$

Shunt resistance for 10°C rise in temperature

 $R_{sh|_{t=10}} = 1.01(1 + 0.00015 \times 10) = 1.0115\Omega$

$$I = I_m \begin{pmatrix} 1 + \frac{R_m}{Rsh} \end{pmatrix}$$

$$100 = I_m \begin{pmatrix} 1 + \frac{101.11}{1.0115} \end{pmatrix}$$

$$I_m t = 10^\circ = 0.9905 mA$$

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Error =(0.9905-1)*100=-0.95%

Example: 1.6

The coil of a 600V M.I meter has an inductance of 1 henery. It gives correct reading at 50HZ and requires 100mA. For its full scale deflection, what is % error in the meter when connected to 200V D.C. by comparing with 200V A.C?

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Solution:

 $V_{m} = 600V, I_{m} = 100mA$ Case-IA.C. $Z_{m} = \frac{V_{m}}{I_{m}} = \frac{600}{=} 6000\Omega \ 0.1$ $X_{L} = 2\Pi fL = 314\Omega$ $R_{m} = \sqrt{Z_{m}^{2} - X^{2}_{L}} = \sqrt{(6000)^{2} - (314)^{2}} = 5990\Omega$ $I_{AC} = \frac{V_{AC}}{Z} = \frac{200}{6000} 33.33mA$ Case-II D.C $I_{DC} = \frac{V_{DC}}{R_{m}} = \frac{200}{5990} 33.39mA$

Error=
$$\frac{I_{DC} - I_{AC} \times 100}{I_{AC}} = \frac{33.39 - 33.33}{33.33} \times 100 = 0.18\%$$

Example: 1.7

A 250V M.I. voltmeter has coil resistance of 500Q, coil inductance Of 1.04 H and series resistance of $2k\Omega$. The meter reads correctively at 250V D.C. What will be the value of capacitance to be used for shunting the series resistance to make the meter read correctly at 50HZ? What is the reading of voltmeter on A.C. without capacitance?

 $C = 0.41 \frac{L}{\left(R_{\rm S}\right)^2}$ Solution :

$$=0.41 \times \frac{\Box 1.04}{(2 \times 10^3)^2} = 0.1 \mu F$$

For A.C $Z = \sqrt{(R_m + R_{Se})^2 + X^2}$

$$Z = \sqrt{(8m + 8s_e)^2 + (314)^2} = 2520\Omega$$

D.C
$$y = 2500\Omega$$

$$500\Omega \rightarrow 250V$$

With D.C

 $R_{total} = 2500\Omega$

For $2500\Omega \rightarrow 250V$

$$1\Omega \rightarrow \frac{250}{2500}$$

$$2520\Omega \rightarrow \frac{250}{250} \times 2520 = 248V$$

Example: 1.8

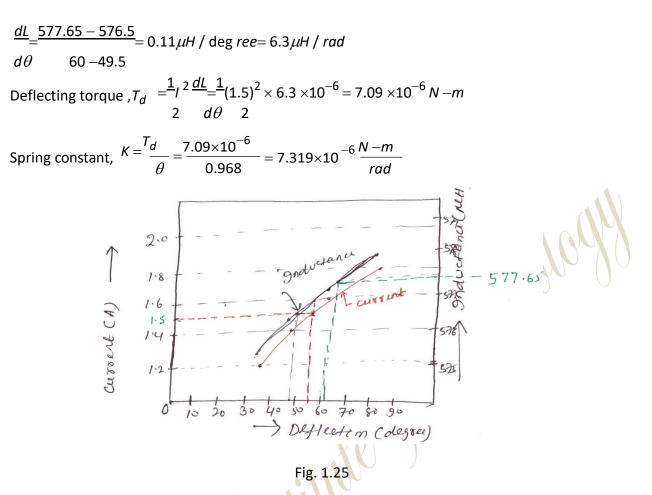
The relationship between inductance of moving iron ammeter, the current and the position of pointer is as follows:

Reading (A)	1.2	1.4	1.6	1.8
Deflection (degree)	36.5	49.5	61.5	74.5
Inductance (μ H)	575.2	576.5	577.8	578.8

Calculate the deflecting torque and the spring constant when the current is 1.5A?

Solution:

For current I=1.5A, θ =55.5 degree=0.96865 rad



Example: 1.9

For a certain dynamometer ammeter the mutual inductance 'M' varies with deflection θ as $M = -6 \cos(\theta + 30^{\circ})mH$.Find the deflecting torque produced by a direct current of 50mA corresponding to a deflection of 60° .

Solution:

$$T = H \frac{dM}{d\theta} + 2^{2} \frac{dM}{d\theta}$$

$$M = -6 \cos(\theta + 30^{\circ})$$

$$\frac{dM}{d\theta} = 6 \sin(\theta + 30)mH$$

$$\frac{dM}{d\theta} = 6 \sin 90 = 6mH / \text{deg}$$

$$T_{d} = H^{2} \frac{2dM}{d\theta} = (50 \times 10^{-3})^{2} \times 6 \times 10^{-3} = 15 \times 10^{-6} N - m$$

Example: 1.10

The inductance of a moving iron

EEI, Semester 4th, Diploma Engineering (Electrical & Electronics) ammeter with a full scale deflection of 90⁰ at 1.5A, is given by the expression $L = 200 + 40\theta - 4\theta^2 - \theta^3 \mu H$, where θ is deflection in radian from the zero position. Estimate the angular deflection of the pointer for a current of 1.0A.

Solution:

 $L = 200 + 40\theta - 4\theta^{2} - \theta^{3}\mu H$ $\frac{dL}{d\theta}\Big|_{\theta=90^{\circ}} = 40 - 8\theta - 3\theta^{2}\mu H / rad$ $\frac{dL}{d\theta}\Big|_{\theta=90^{\circ}} = 40 - 8 \times \frac{\Pi}{2} - \frac{\Pi}{3(\frac{1}{2})}\mu H / rad = 20\mu H / rad$ $\therefore \theta = \frac{1}{2K}I^{2}\left(\frac{dL}{d\theta}\right)$ $\frac{\Pi}{2} = \frac{1}{2K}I^{2}\left(\frac{dL}{d\theta}\right)$ $K=\text{Spring constant} = 14.32 \times 10^{-6} N - m / rad$ For I=1A, $\therefore \theta = \frac{1}{2K}I^{2}\left(\frac{dL}{d\theta}\right)$ $\therefore \theta = \frac{1}{2} \times \frac{(1)^{2}}{2K}\left(\frac{dU}{d\theta}\right)$ $\therefore \theta = \frac{1}{2} \times \frac{(1)^{2}}{14.32 \times 10^{-6}}\left(40 - 8\theta - 3\theta^{2}\right)$ $3\theta + 36.64\theta^{2} - 40 = 0$ $\theta = 1.008rad, 57.8^{\circ}$

Example: 1.11

The inductance of a moving iron instrument is given by

the deflection in radian from zero position. The spring constant is $12 \times 10^{-6} N - m / rad$. Estimate the deflection for a current of 5A.

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Solution:

∴ *θ*= 1.69*rad*,96.8[°]

Example: 1.12

The following figure gives the relation between deflection and inductance of a moving iron instrument.

Deflection (degree) 20 30 40 50 60 70 80 90 355.5366.5 376.5385 Inductance (μH) 335 345 391.2396.5 Find the current and the torque to give a deflection of (a) 30° (b) 80° . Given that control spring constant is $0.4 \times 10^{-6} N - m / \text{deg } ree$

Solution:

$$\theta = \frac{1}{2K} I^2 \left(\frac{dL}{d\theta} \right)$$

(a) For $\theta = 30^{\circ}$

The curve is linear

$$\therefore \left(\frac{dL}{d\theta}\right)_{\theta=30} = \frac{355.5 - 335}{40 - 20} = 1.075 \mu H / \deg ree = 58.7 \mu H / rad$$

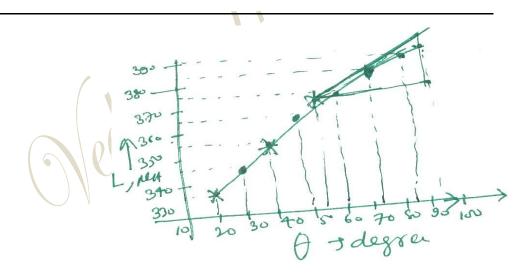


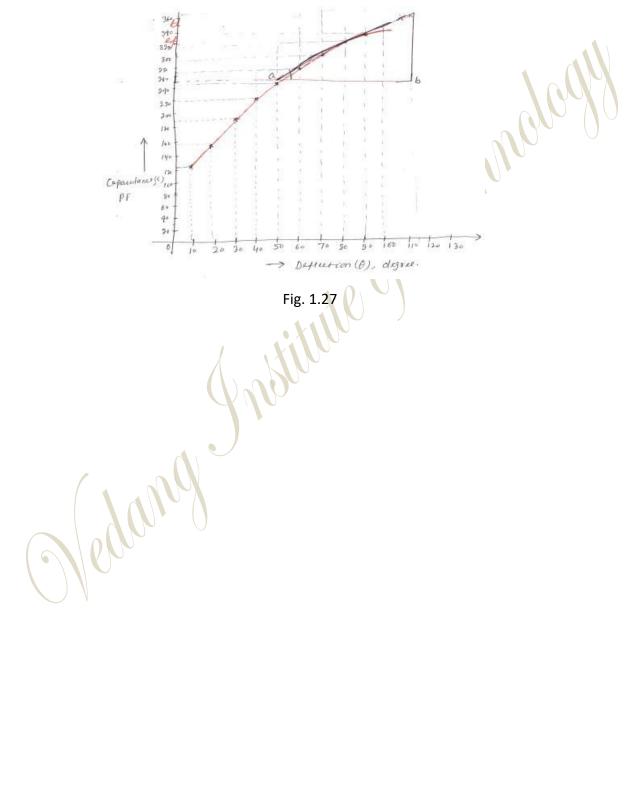
Fig. 1.26

Example: 1.13

 $In an electrostatic voltmeter the full scale deflection is obtained when the moving plate turns through 90^{0}. The torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the angle of the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the angle of the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the angle of the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the torsional constant is 10 \times 10^{-6} N-m/rad. The relation between the torsional constant is 10 \times$

deflection and capacitance between the fixed and moving plates is given by										
Deflection (degree)	0	10	20	30	40	50	60	70	80	90
Capacitance (PF)	81.4	121	156	189.2	220	246	272	294	316	334
Find the voltage applied to the instrument when the deflection is 90 ⁰ ?										

Solution:



$$\frac{dC}{d\theta} = \tan \theta = \frac{bc}{d\theta} = \frac{370 - 250}{ab} = 1.82PF / \deg ree = 104.2PF / rad$$

Spring constant $K = 10 \times 10^{-6} \frac{N - m}{m} = 0.1745 \times 10^{-6} N - m / \text{deg ree rad}$

$$\theta = \frac{1}{2K} V^{2} \left(\frac{dC}{d\theta} \right) \Rightarrow V = \frac{2K\theta}{\sqrt{\frac{dC}{d\theta}}}$$
$$V = \sqrt{\frac{2 \times 0.1745 \times 10^{-6} \times 90}{104.2 \times 10^{-12}}} = 549 \text{ volt}$$

Example: 1.14

Design a multi range d.c.mille ammeter using a basic movement with an internal resistance

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 $I_m = 1mA$. The ranges required are 0-10mA; 0-50mA; $R_m = 50\Omega$ and a full scale deflection current

0-100mA and 0-500mA.

Multiplying power $m = \begin{bmatrix} I \\ I_m \end{bmatrix} = \begin{bmatrix} 10 \\ 1 \end{bmatrix} = \begin{bmatrix} 10 \\ I_m \end{bmatrix}$ \therefore Shunt resistance $R_{sh1} = \frac{R_m}{m-1} = \frac{50}{10-1} = 5.55\Omega$ **Case-II**0-50mA $m = \frac{50}{1} = 50$ $R_{sh2} = \frac{R_m}{m-1} = \frac{50}{50-1} = 1.03\Omega$ **Case-III** 0-100mA, $m = \frac{100}{1} = 100\Omega$ $R_{sh3} = \frac{R_m}{m-1} = \frac{50}{100 - 1} = 0.506\Omega$ **Case-IV** 0-500mA, $m = \frac{500}{=500\Omega}$ $R_{sh4} = \frac{R_m}{m-1} = \frac{50}{500-1} = 0.1\Omega$

Eaxmple 1.15

A moving coil voltmeter with a resistance of 20Ω gives a full scale deflection of 120^{0} , when a potential difference of 100mV is applied across it. The moving coil has dimension of 30mm*25mm and is wounded with 100 turns. The control spring constant is

 $0.375 \times 10^{-6} N - m/\text{degree}$. Find the flux density, in the airgap. Find also the diameter of copper wire of coil winding if 30% of instrument resistance is due to coil winding. The specific resistance for copper = $1.7 \times 10^{-8} \Omega m$. echno

Solution:

Data given

 $V_{m} = 100 mV$

 $R_m = 20\Omega$

N=100

$$\theta = 120^{\circ}$$
N=100
$$K = 0.375 \times 10^{-6} N - m / \deg ree$$

$$R_{C} = 30\% of R_{m}$$

$$\rho = 1.7 \times 10^{-8} \Omega m$$

$$I_{m} = -\frac{V_{m}}{R_{m}} = -3$$

 $R_C = 30\% of R_m$

 $\rho = 1.7 \times 10^{-8} \Omega m$

$$I_m = \frac{V_m}{R_m} = 5 \times 10^{-3} A$$

$$T_d = BANI, T_c = K\theta = 0.375 \times 10^{-6} \times 120 = 45 \times 10^{-6} N - m$$
$$B = \frac{T_d}{ANI} = \frac{45 \times 10^{-6}}{30 \times 25 \times 10^{-6} \times 100 \times 5 \times 10^{-3}} = 0.12 wb/m^2$$

$$R_C = 0.3 \times 20 = 6\Omega$$

Length of mean turn path =2(a+b)=2(55)=110mm

$$R_{C} = N \begin{vmatrix} \underline{\rho} \\ A \end{vmatrix}$$
$$A = \frac{N \times \rho \times (l_{t})}{R_{C}} = \frac{100 \times 1.7 \times 10^{-8} \times 110 \times 10^{-3}}{6}$$

$$= 3.116 \times 10^{-8} m^2$$

$$= 31.16 \times 10^{-3} mm^2$$

 $A = -d^2 \Rightarrow d = 0.2mm 4$

Example: 1.16

A moving coil instrument gives a full scale deflection of 10mA, when the potential difference across its terminal is 100mV. Calculate

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- (1) The shunt resistance for a full scale deflection corresponding to100A neu
- (2) The resistance for full scale reading with 1000V.

Calculate the power dissipation in eachcase?

Solution:

Data given

 $I_m = 10 mA$ $V_{m} = 100 mV$ I = 100 A $I = I_m \begin{vmatrix} R_m \\ 1 + R_m \end{vmatrix}$ $100=10\times10 \begin{bmatrix} -3 & 10 \\ 1+ & R \end{bmatrix}$ $R_{sh} = 1.001 \times 10^{-3} \Omega$ *R_{se}* =??,*V*=1000*V* $R_{m} = \frac{V_{m}}{I} = \frac{100}{10} = 10\Omega$ 10 $V = V_m | 1 +$ $1000 = 100 \times 10^{-3} (1 + R_{se})$

 $\therefore R_{se} = 99.99K\Omega$

Example: 1.17

Design an Aryton shunt to provide an ammeter with current ranges of 1A,5A,10A and 20A. A basic meter with an internal resistance of 50w and a full scale deflection current of 1mA is to be used.

Sector

Solution: Data given

$$m_{1} = \frac{l_{1}}{l_{m}} = 1000 A$$

$$m_{1} = \frac{l_{1}}{l_{m}} = 1000 A$$

$$m_{2} = \frac{l_{2}}{l_{m}} = 5000 A$$

$$m_{3} = \frac{l_{3}}{l_{m}} = 10000 A$$

$$m_{4} = \frac{l_{4}}{l_{m}} = 20000 A$$

$$R_{sh1} = \frac{R_m}{m_1 - 1} = \frac{\Box 50}{1} = 0.05\Omega 1000 - 1$$
$$R_{sh2} = \frac{R_m}{m_2 - 1} = \frac{\Box 50}{5000 - 1} = 0.01\Omega$$
$$R_{sh3} = \frac{R_m}{m_3 - 1} = \frac{50}{10000 - 1} = 0.005\Omega$$
$$R_{sh4} = \frac{R_m}{m_4 - 1} = \frac{\Box 50}{-1} = 0.0025\Omega 20000$$

 \therefore The resistances of the various section of the universal shunt are

 $R_1 = R_{sh1} - R_{sh2} = 0.05 - 0.01 = 0.04\Omega$ $R_2 = R_{sh2} - R_{sh3} = 0.01 - 0.005 = 0.005\Omega R_3$ $= R_{sh3} - R_{sh4} = 0.005 - 0.025 = 0.0025\Omega R_4$ $= R_{sh4} = 0.0025\Omega$

Example: 1.18

A basic d' Arsonval meter movement with an internal resistance $R_m = 100\Omega$ and a full scale current $I_m = 1mA$ is to be converted in to a multi range d.c. voltmeter with ranges of 0-10V, 0of

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50V, 0-250V, 0-500V. Find the values of various resistances using the potential divider arrangement.

Solution: Data given

 $R_m = 100\Omega$ $I_m = 1mA$ $V_m = I_m \times R_m$ $V_m = 100 \times 1 \times 10^{-3}$

 $V_{m} = 100 mV$

 $m_{I} = \frac{V_{1}}{V_{m}} = \frac{\Box 10}{100 \times 10^{-3}} = 100$ $m_{2} = \frac{V_{2}}{V_{m}} = \frac{\Box 50}{100 \times 10^{-3}} = 500$ 100×10^{-3} $m_{3} = \frac{V_{3}^{'''}}{V_{m}} = \frac{250}{100} = 2500$ $m_{4} = \frac{V_{4}}{V_{m}} = \frac{100}{100 \times 10^{-3}} = 5000$

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 $R_1 = (m_1 - 1)R_m = (100 - 1) \times 100 = 9900\Omega$ $R_2 = (m_2 - m_1)R_m = (500 - 100) \times 100 = 40K\Omega$ $R_3 = (m_3 - m_2)R_m = (2500 - 500) \times 100 = 200K\Omega$ $R_4 = (m_4 - m_3)R_m = (5000 - 2500) \times 100 = 250K\Omega$

AC BRIDGES

2.1 General form of A.C.bridge

AC bridge are similar to D.C. bridge in topology(way of connecting). It consists of four arm AB, BC, CD and DA . Generally the impedance to be measured is connected between 'A' and 'B'. A detector is connected between 'B' and 'D'. The detector is used as null deflection instrument. Some of the arms are variable element. By varying these elements, the potential values at 'B' and 'D' can be made equal. This is called balancing of thebridge.

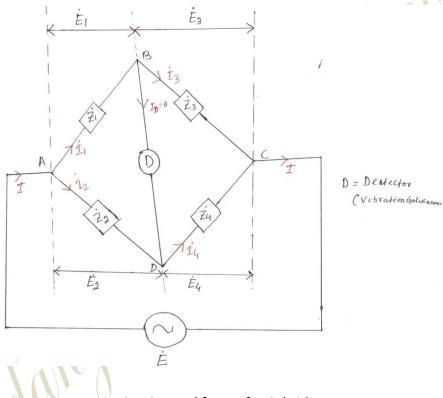


Fig. 2.1 General form of A.C. bridge

At the balance condition, the current through detector iszero.

$$\therefore I_{1} = I_{3}$$

$$\therefore I_{2} = I_{4}$$

$$\therefore I_{1} = I_{3}$$

$$\vdots$$

$$I_{2} = I_{4}$$

$$\vdots$$

$$I_{2} = I_{4}$$

(2.1)

At balance condition,

Voltage drop across 'AB'=voltage drop across 'AD'.

$$E_1 = E_2$$

$$\therefore I_1 Z_1 = I_2 Z_2$$
(2.2)
Similarly, Voltage drop across 'BC' = voltage drop across 'DC'
$$E_3 = E_4$$

$$\therefore I_3 Z_3 = I_4 Z_4$$
(2.3)
From Eqn. (2.2), we have $\therefore \frac{I_1}{I_2} = \frac{Z_2}{I_1}$
(2.4)
From Eqn. (2.3), we have $\therefore \frac{I_3 = Z_4}{I_4 = Z_3}$
(2.5)

From equation -2.1, it can be seen that, equation -2.4 and equation-2.5 are equal.

$$\begin{array}{c} \cdot \cdot \underline{Z}_{2} \underline{Z}_{4} \\ \cdot \cdot \underline{Z}_{1} \\ Z_{1} \\ Z_{3} \end{array}$$

 $\therefore Z_1 Z_4 = Z_2 Z_3$

Products of impedances of opposite arms are equal.

$$\therefore \mathbf{Z}_1 \not\downarrow \theta_1 \mathbf{Z}_4 \not\downarrow \theta_4 = \mathbf{Z}_2 \not\angle \theta_2 \mathbf{Z}_3 \not\downarrow \theta_3$$

$$\Rightarrow \not z_1 Z_4 \square \theta_1 + \theta_4 = Z_2 \not z_3 \square \theta_2 |+ \theta_3|$$

 $|Z_1 Z_4| = 2_2 Z_3$

 $\theta_1 + \theta_4 = \theta_2 + \theta_3$

- * For balance condition, magnitude on either side must beequal.
- * Angle on either side must beequal.

<u>Summary</u>

For balance condition,

- $I_1 = I_3, I_2 = I_4$
- $|Z_1 Z_4| = |Z_2 Z_3|$
- $\theta_1 + \theta_4 = \theta_2 + \theta_3$
- E₁=E₂ & E₃=E₄

2.2 Types of detector

The following types of instruments are used as detector in A.C. bridge.

- Vibrationgalvanometer
- Head phones (speaker)
- Tunedamplifier

2.2.1 Vibrationgalvanometer

Between the point 'B' and 'D' a vibration galvanometer is connected to indicate the bridge balance condition. This A.C. galvanometer which works on the principle of resonance. The A.C. galvanometer shows a dot, if the bridge is unbalanced.

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2.2.2 Headphones

Two speakers are connected in parallel in this system. If the bridge is unbalanced, the speaker produced more sound energy. If the bridge is balanced, the speaker do not produced any soundenergy.

2.2.3 Tunedamplifier

If the bridge is unbalanced the output of tuned amplifier is high. If the bridge is balanced, output of amplifier is zero.

2.3 Measurements of inductance

2.3.1 Maxwell's inductancebridge

The choke for which R_1 and L_1 have to measure connected between the points 'A' and 'B'. In this method the unknown inductance is measured by comparing it with the standard inductance.

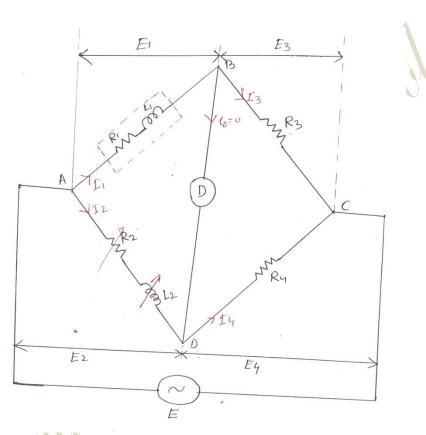


Fig. 2.2 Maxwell's inductance bridge

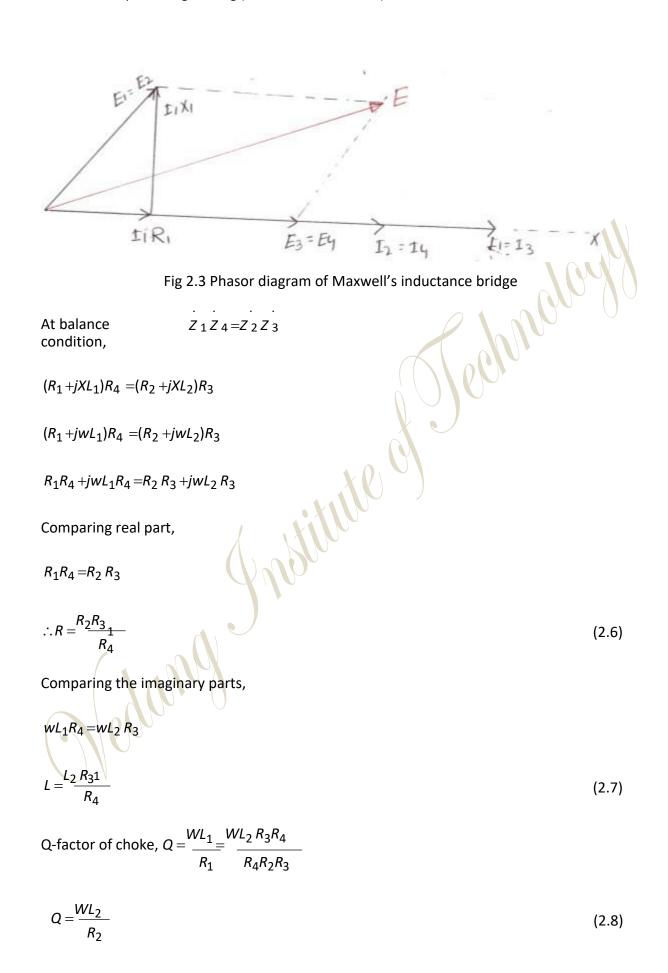
 L_2 is adjusted, until the detector indicates zero current.

Let R₁= unknown resistance

 L_1 = unknown inductance of the choke.

L₂= known standard inductance

 R_1, R_2, R_4 = known resistances.



Advantages

- \checkmark Expression for R₁ and L₁are simple.
- ✓ Equations areasimple
- ✓ They do not depend on the frequency (as w iscancelled)
- ✓ R_1 and L_1 are independent of eachother.

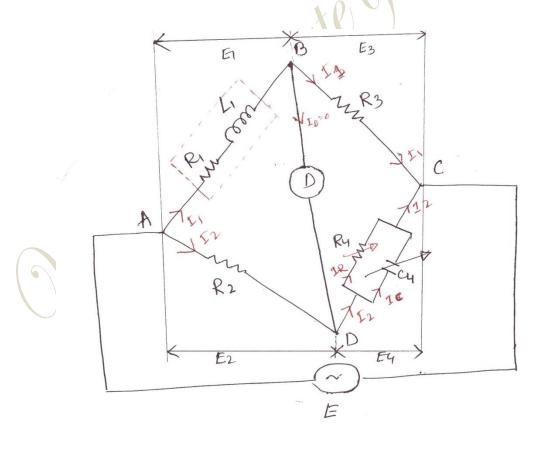
Disadvantages

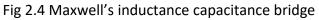
- ✓ Variable inductor iscostly.
- ✓ Variable inductor isbulky.

2.3.2 Maxwell's inductance capacitancebridge

Unknown inductance is measured by comparing it with standard capacitance. In this bridge, balance condition is achieved by varying C_4 .

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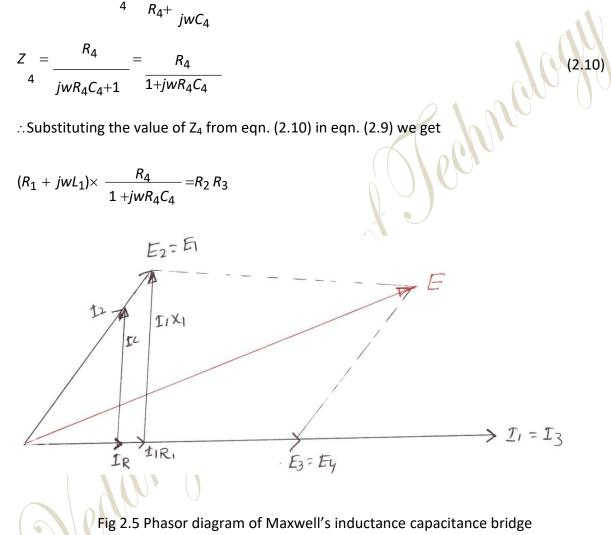




$$Z_{4} = R_{4} \mid \mid \frac{1}{jwC_{4}} = \frac{R_{4} \times \frac{1}{jwC_{4}}}{R_{4} + \frac{1}{jwC_{4}}}$$

$$Z_{4} = \frac{R_{4}}{jwR_{4}C_{4}+1} = \frac{R_{4}}{1+jwR_{4}C_{4}}$$

 \therefore Substituting the value of Z4 from eqn. (2.10) in eqn. (2.9) we get



$$(R_1 + jwL_1)R_4 = R_2 R_3 (1 + jwR_4C_4)$$

 $R_1R_4 + jwL_1R_4 = R_2R_3 + jwC_4R_4R_2R_3$

Comparing real parts,

 $R_1 R_4 = R_2 R_3$

(2.9)

$$\Rightarrow R = \frac{R_2 R_3}{1 R_4}$$
(2.11)

Comparing imaginary part,

 $wL_1R_4 = wC_4R_4R_2R_3$

$$L_1 = C_4 R_2 R_3$$

Q-factor of choke,

$$Q = \frac{WL_1}{R_1} = w \times C \quad {}_4R_2R_3 \times \frac{R_4}{R_2R_3}$$

$$Q = wC_4R_4$$

Advantages

- ✓ Equation of L_1 and R_1 are simple.
- ✓ They are independent offrequency.
- ✓ They are independent of eachother.
- ✓ Standard capacitor is much smaller in size than standardinductor.

Disadvantages

- ✓ Standard variable capacitance iscostly.
- ✓ It can be used for measurements of Q-factor in the ranges of 1 to10.
- \checkmark It cannot be used for measurements of choke with Q-factors more
 - than 10. We know that $Q=wC_4R_4$

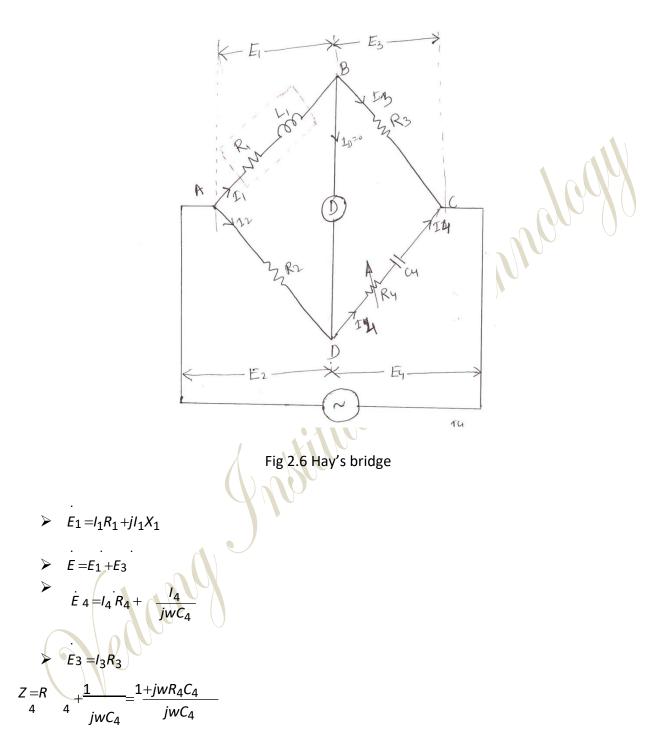
For measuring chokes with higher value of Q-factor, the value of C_4 and R_4 should be higher. Higher values of standard resistance are very expensive. Therefore this bridge cannot be used for higher value of Q-factor measurements.

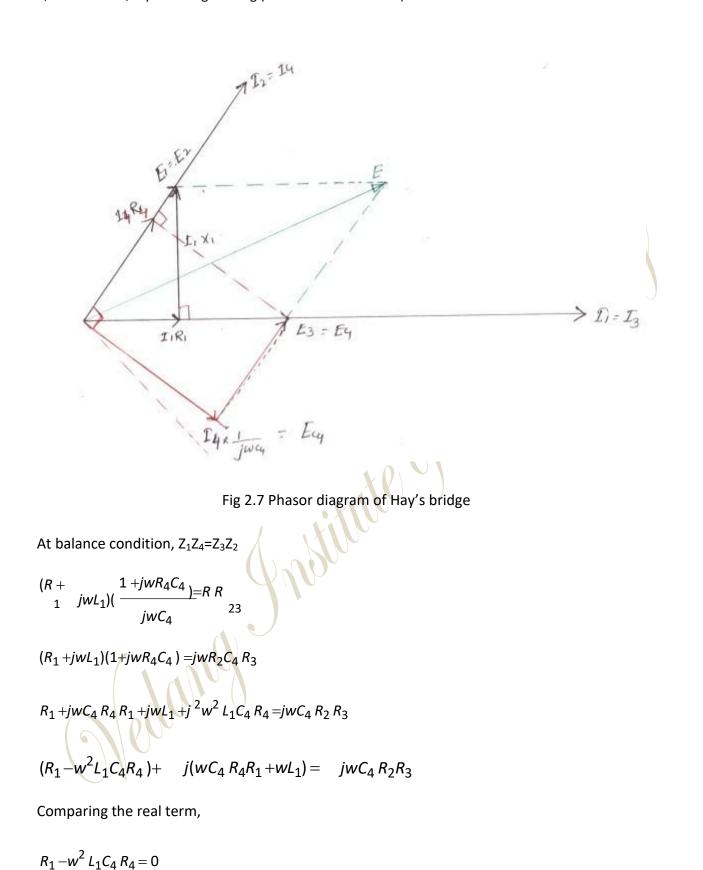
(2.12)

'ephologic

(2.13)

2.3.3 Hay'sbridge





 $R_1 = w^2 L_1 C_4 R_4 \tag{2.14}$

Comparing the imaginary terms,

$$wC_4R_4R_1 + wL_1 = wC_4R_2R_3$$

$$C_4 R_4 R_1 + L_1 = C_4 R_2 R_3$$

$$L_1 = C_4 R_2 R_3 - C_4 R_4 R_1$$

Substituting the value of R_1 fro eqn. 2.14 into eqn. 2.15, we have,

$$L_{1} = C_{4}R_{2}R_{3} - C_{4}R_{4} \times w^{2}L_{1}C_{4}R_{4}$$

$$L_{1} = C_{4}R_{2}R_{3} - w^{2}L_{1}C_{4}^{2}R_{4}^{2}$$

$$L_{1}(1+w^{2}L_{1}C_{4}^{2}R_{4}^{2}) = C_{4}R_{2}R_{3}$$

$$L_{T} = \frac{C_{4}R_{2}R_{3}}{1+w^{2}L_{1}C_{1}^{2}R_{4}^{2}}$$

$$(2.16)$$
Substituting the value of L₁ in eqn. 2.14, we have
$$R_{1} = \frac{w^{2}C_{4}^{2}R_{2}R_{3}R_{4}}{1+w^{2}C_{4}^{2}R_{4}^{2}}$$

$$(2.17)$$

(2.15)

$$Q = \frac{wL_{1}}{R_{1}} = \frac{w \times C_{4} R_{2} R_{3}}{1 + w^{2} C_{4}^{2} R_{4}^{2}} \times \frac{1 + w^{2} C_{4}^{2} R_{4}^{2}}{w^{2} C_{4}^{2} R_{4} R_{2} R_{3}}$$

$$Q = \frac{1}{wC_{4} R_{4}}$$
(2.18)

Advantages

- ✓ Fixed capacitor is cheaper than variablecapacitor.
- ✓ This bridge is best suitable for measuring high value ofQ-factor.

Disadvantages

- ✓ Equations of L1and R1 arecomplicated.
- ✓ Measurements of R_1 and L_1 require the value offrequency.
- ✓ This bridge cannot be used for measuring low Q-factor.

2.3.4 Owen'sbridge

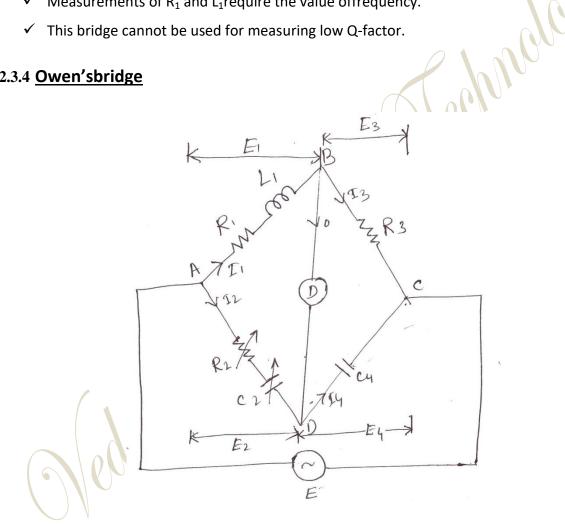


Fig 2.8 Owen's bridge

- $E_1 = I_1 R_1 + j I_1 X_1$
- \succ I₄ leads E₄ by 90⁰

$$\succ$$
 $E = E_1 + E_3$

$$E_2 = I_2 R_2 + \frac{I_2}{j w C_2}$$

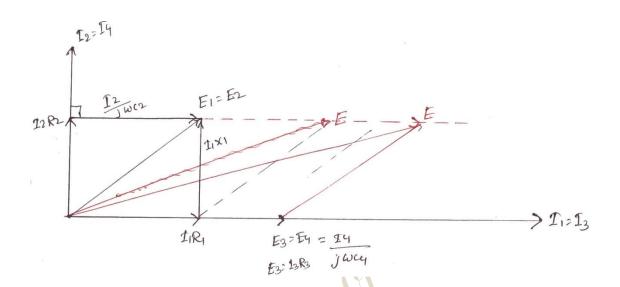


Fig 2.9 Phasor diagram of Owen's bridge

Balance condition,
$$Z_1 Z_4 = Z_2 Z_3$$

 $Z_2 = R_2 + \frac{1}{jwC_2} = \frac{jwC_2 R_2 + 1}{jwC_2}$
 $\therefore (R_1 + jwL) \times \frac{1}{jwC_4} = \frac{(1 + jwR_2 C_2) \times R_3}{jwC_2}$
 $C_2 (R_1 + jwL_1) = R_3 C_4 (1 + jwR_2 C_2)$
 $R_1 C_2 + jwL_1 C_2 = R_3 C_4 + jwR_2 C_2 R_3 C_4$

Comparing real terms,

$$R_1C_2 = R_3C_4$$

$$R = \frac{R_3 C_4 1}{C_2}$$

Comparing imaginary terms,

$$wL_1C_2 = wR_2C_2R_3C_4$$

 $L_1 = R_2 R_3 C_4$

Q- factor =
$$\frac{WL_1}{R_1} = \frac{WR_2R_3C_4C_2}{R_3C_4}$$

 $Q = wR_2C_2$

Advantages

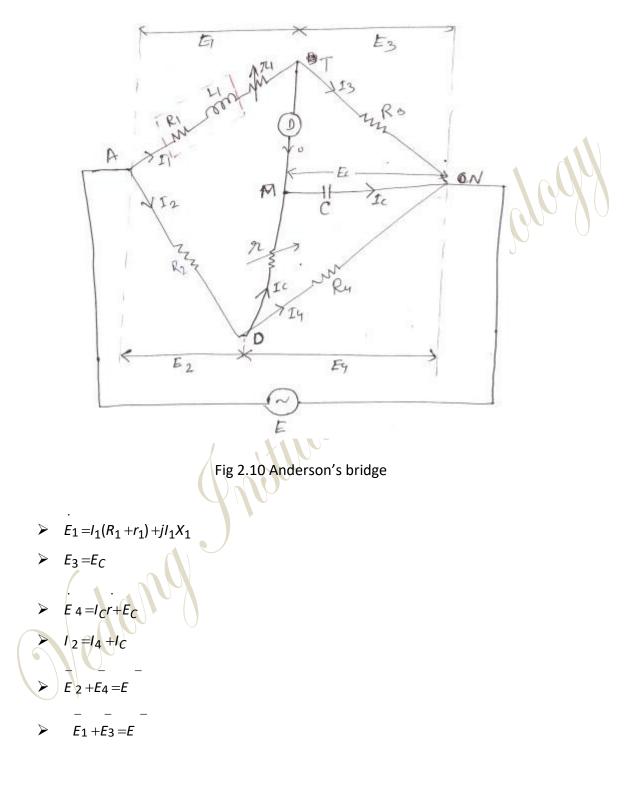
- \checkmark Expression for R₁ and L₁ aresimple.
- itute C \checkmark R₁ and L₁are independent of Frequency.

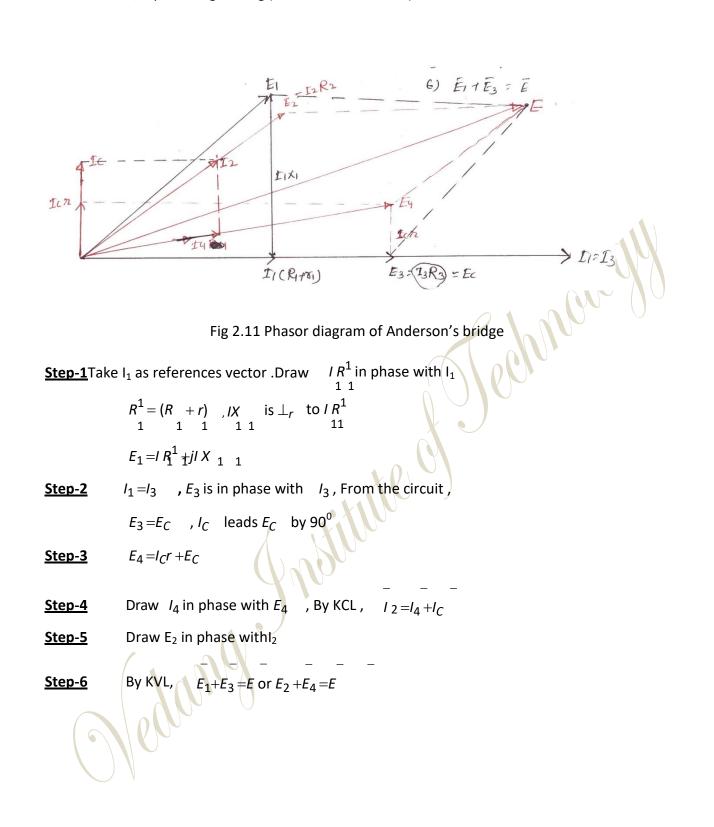
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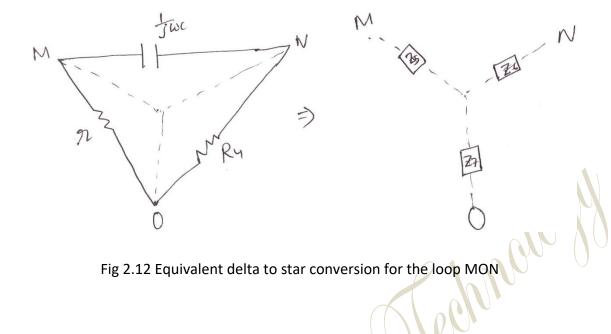
Disadvantages

- ✓ The Circuits used twocapacitors.
- ✓ Variable capacitor iscostly.
- ✓ Q-factor range isrestricted.

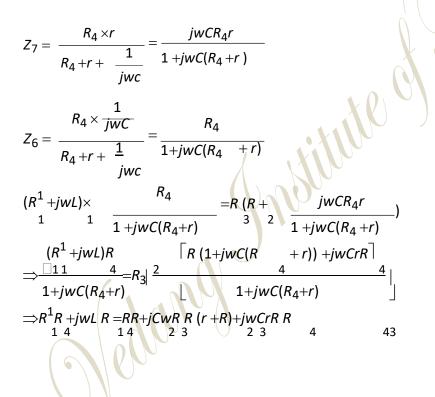
2.3.5 Anderson'sbridge

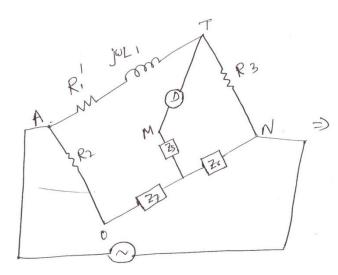






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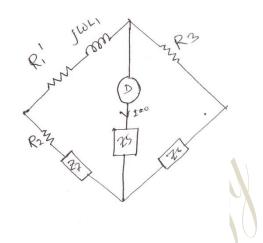


Fig 2.13 Simplified diagram of Anderson's bridge

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Comparing real term,

 $R_{1 4}^{1}R = RR_{23}$

 $(R_1 + r_1)R_4 = R_2 R_3$ $R = \frac{R_2 R_3}{r_1} - r_1$

$$1 \frac{1}{R_4} 1$$

Comparing the imaginary term,

$$wL_{1}R_{4} = wCR_{2}R_{3}(r + R_{4}) + wcrR_{3}R_{4}$$

$$L = \frac{R_{2}R_{3}C}{1}(r + R) + RrC$$

$$L = RC \frac{R_{4}}{R_{2}}(r + R) + r$$

$$L = RC \frac{R_{2}}{R_{4}}(r + R) + r$$

Advantages

- ✓ Variable capacitor is notrequired.
- ✓ Inductance can be measuredaccurately.
- ✓ R_1 and L_1 are independent offrequency.
- ✓ Accuracy is better than otherbridges.

Disadvantages

- ✓ Expression for R_1 and L_1 are complicated.
- ✓ This is not in the standard form A.C.bridge.

2.4 Measurement of capacitance and loss angle. (Dissipationfactor)

2.4.1 Dissipation factors(D)

A practical capacitor is represented as the series combination of small resistance and idealcapacitance.

From the vector diagram, it can be seen that the angle between voltage and current is slightly less than 90° . The angle ' δ is called loss angle.

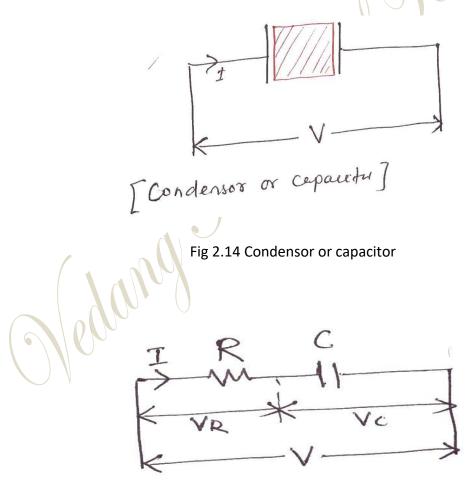


Fig 2.15 Representation of a practical capacitor

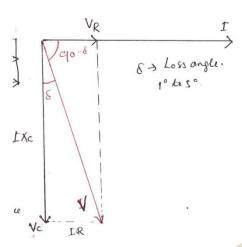


Fig 2.16 Vector diagram for a practical capacitor

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A dissipation factor is defined as 'tan δ .

 $\therefore \tan \delta = \frac{IR}{IX_C} = \frac{R}{-w}CR X_C$ D = wCR $D = \frac{1}{Q}$

 $D = \tan \delta = \frac{\sin \delta}{\cos \delta} \cong \frac{\delta}{1}$ For small value of ' δ in radians

 $D \cong \delta \cong$ LossAngle (' δ must be inradian)

2.4.2 Desauty'sBridge

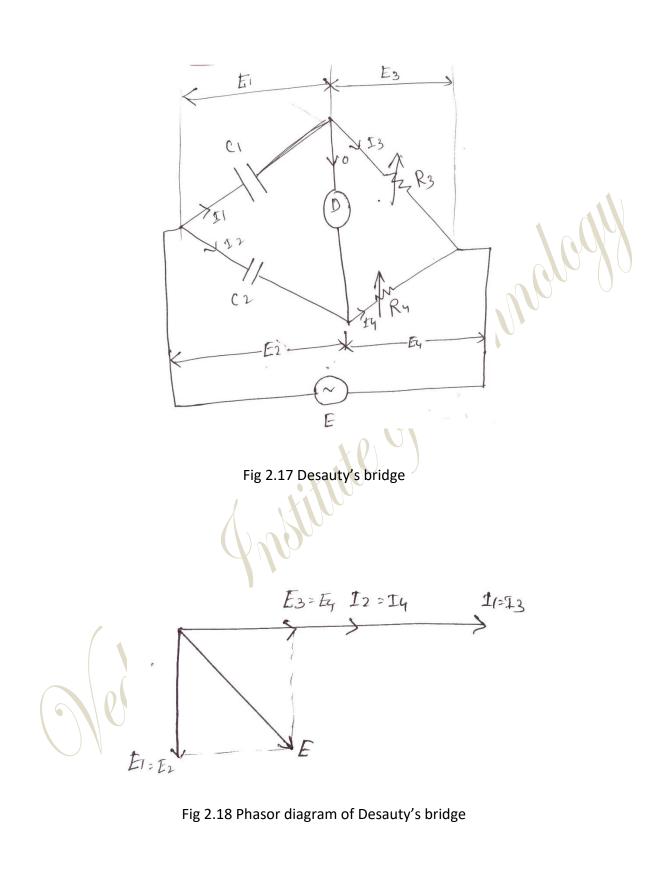
C₁= Unknown capacitance

At balance condition,

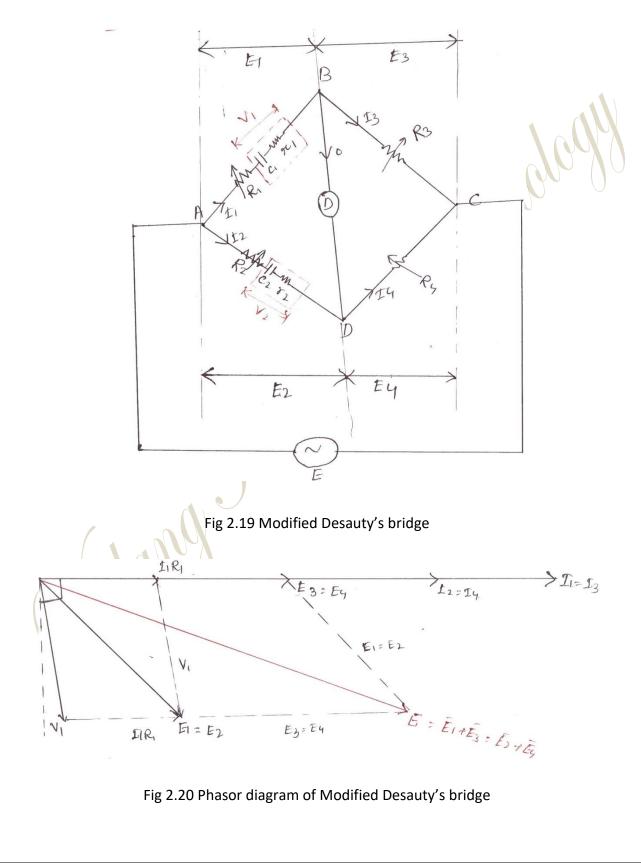
$$\frac{1}{jwC_1} \times R_4 = \frac{1}{jwC_2} \times R_3$$

$$\frac{R_4}{C_1} = \frac{R_3}{C_2}$$

$$\Rightarrow C = \frac{R_4 C_2}{\frac{1}{R_3}}$$



2.4.3 Modified desauty'sbridge



 $R_{1}^{1} = (R + r)$ $R_{2}^{1} = R(R + r)$ $R_{1}^{1} = R(R + r)$ $R_{$

rechnolog)

Comparing imaginary term,

$$\frac{R_4}{wC_1} = \frac{R_3}{wC_2}$$

$$C = \frac{R_4 C_2 1}{R_3}$$

Dissipation factor D=wC₁r₁

Advantages

 \checkmark r₁ and c₁ are independent offrequency.

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- ✓ They are independent of eachother.
- ✓ Source need not be pure sinewave.

2.4.4 Scheringbridge

 $E_1 = I_1 r_1 - j I_1 X_4$

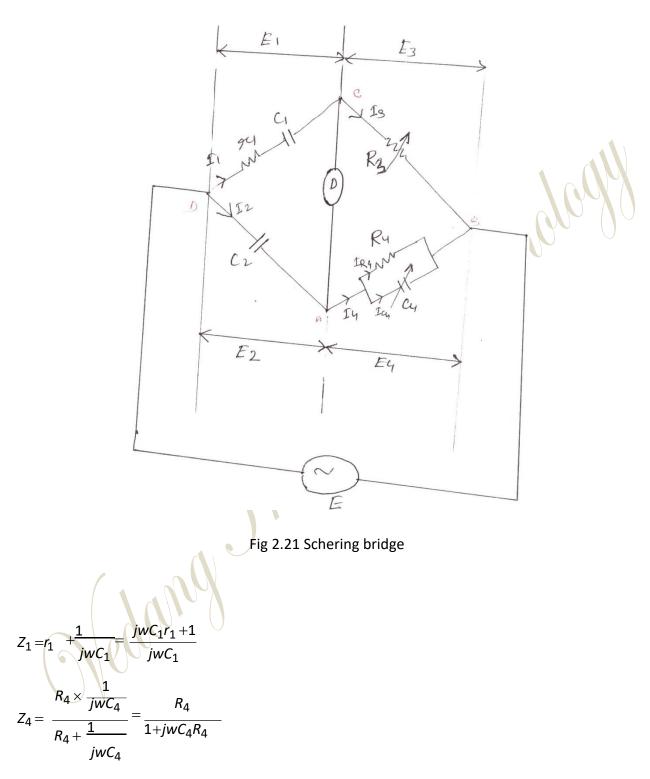
C₂ = C₄= Standard capacitor (Internal resistance=0)

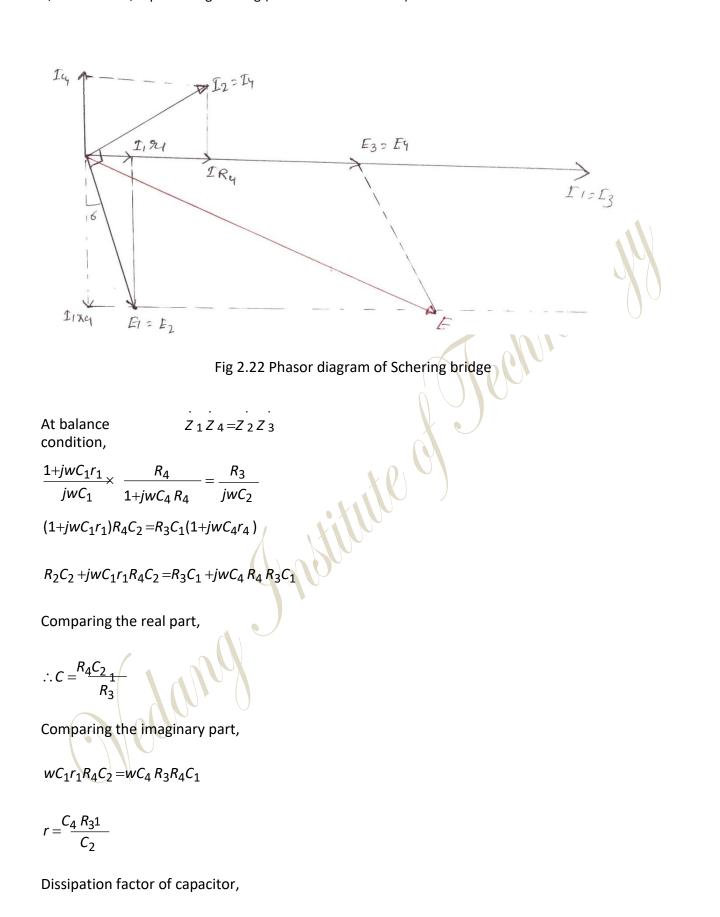
C₄= Variable capacitance.

C₁= Unknown capacitance.

r₁= Unknown series equivalent resistance of the capacitor.

R₃=R₄= Known resistor.





$$D = wCr = w \times \frac{R_4C_2 \times C_4 R_3}{R_3} - \frac{C_2}{C_2}$$

 $\therefore D = wC_4 R_4$

Advantages

- ✓ In this type of bridge, the value of capacitance can be measured accurately.
- ✓ It can measure capacitance value over a widerange.
- ✓ It can measure dissipation factoraccurately.

Disadvantages

- ✓ It requires twocapacitors.
- ✓ Variable standard capacitor iscostly.

2.5 Measurements of frequency

2.5.1 Wein'sbridge

Wein's bridge is popularly used for measurements of frequency of frequency. In this bridge, the value of all parameters are known. The source whose frequency has to measure is connected as shown in the figure.

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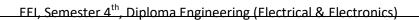
$$Z_{1} = r_{1} + \frac{1}{jwC_{1}} = \frac{jwC_{1}r_{1} + 1}{jwC_{1}}$$

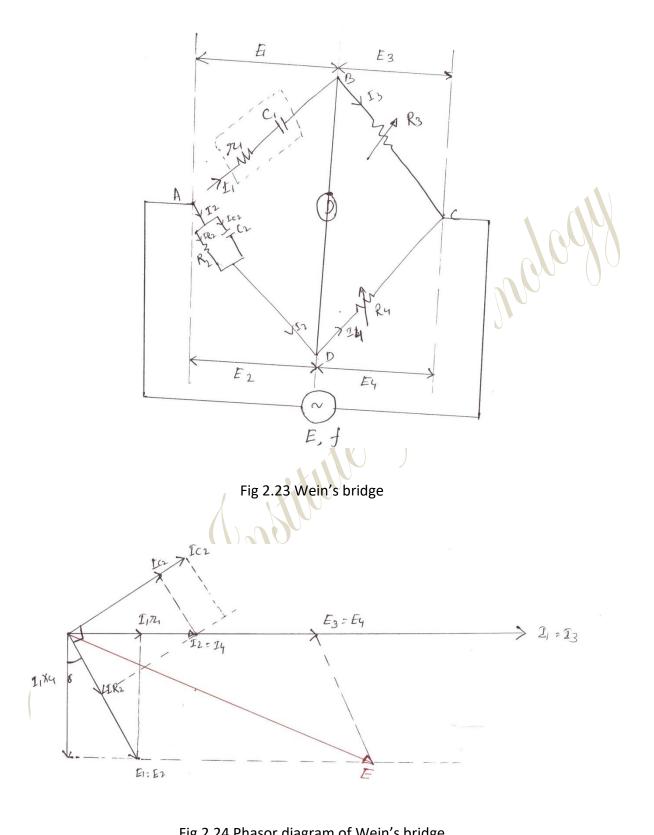
$$Z_{2} = \frac{R_{2}}{1 + jwC_{2}R_{2}}$$
At balance $Z_{1}Z_{4} = Z_{2}Z_{3}$
condition, $R_{2} \times R$

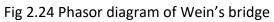
$$\frac{jwC_{1}r_{1}+1}{jwC_{1}} \times R_{4} = \frac{1}{1+jwC_{2}R_{2}} \times R_{3}$$

$$(1+jwC_{1}r_{1})(1+jwC_{2}R_{2})R_{4} = R_{2}R_{3} \times jwC_{1}$$

$$\left[1+jwCR_{2} + jwCr_{11} - w^{2}CCrR_{1212}\right] = jwC_{11}\frac{R_{2}R_{3}}{R_{4}}$$







Comparing real
term,
$$1 - w^2 C_1 C_2 r_1 R_2$$

= 0
 $w^2 C_1 C_2 r_1 R_2 = 1$
 $w^2 = \frac{1}{C_1 C_2 r_1 R_2}$
 $w = \frac{1}{\sqrt{C_1 C_2 r_1 R_2}}, f = \Box^1 2 \Pi \zeta_1 C_2 r_1 R_2$

<u>NOTE</u>

Mala The above bridge can be used for measurements of capacitance. In such case, r₁ and C₁ are unknown and frequency is known. By equating real terms, we will get R₁ and C₁. Similarly by equating imaginary term, we will get another equation in terms of r_1 and C_1 . It is only used for stitute measurements of Audio frequency.

A.F=20 HZ to 20 KHZ

R.F=>> 20 KHZ

Comparing imaginary term,

$$wC_{2}R_{2} + wC_{1}r_{1} = wC_{1} \frac{R_{2}R_{3}}{R_{4}}$$

$$C_{2}R_{2} + C_{1}r_{1} = \frac{C_{1}R_{2}R_{3}}{R_{4}}$$

$$C_{1} = \frac{1}{w^{2}C r R_{2}}$$
(2.19)

Substituting in eqn. (2.19), we have

 $\frac{r_1}{w^2 C \frac{r_R}{212}} = \frac{R_2 R_3}{R_4} C_1$ СŖђ

Multiplying $\frac{R_4}{R_2 R_3}$ in both sides, we have

$$C_{2} \xrightarrow{R_{2}} \frac{R_{4}}{R_{2}R_{3}} + \frac{1}{w^{2}C_{2}R_{2}} \times \frac{R_{4}}{R_{2}R_{3}} = C_{1}$$

$$C_{1} = \frac{C_{2}R_{4}}{R_{3}} - \frac{w^{2}C_{2}R_{4}^{R_{2}}R}{223}$$

$$w^{2}C_{1}r_{1}C_{2}R_{2} = 1$$

$$r_{1} = \frac{1}{w^{2}C_{2}R_{2}C_{1}} - \frac{w^{2}C_{2}R_{2}}{w^{2}C_{2}R_{2}} \left[\frac{C_{2}R_{4}}{R_{2}} + \frac{w^{2}C_{1}R_{4}}{2g_{3}^{2}R_{1}} \right]$$

$$= \frac{1}{\left[\frac{w^{2}C_{2}^{2}R_{2}R_{4}+R_{4}}{R_{3}} + \frac{1}{R_{2}R_{3}} \right]}$$

$$\therefore r_{1} = \frac{1}{R_{4}} \left[\frac{w^{2}C_{2}^{2}R_{2}}{22} + \frac{1}{R_{2}} \right]^{1}$$

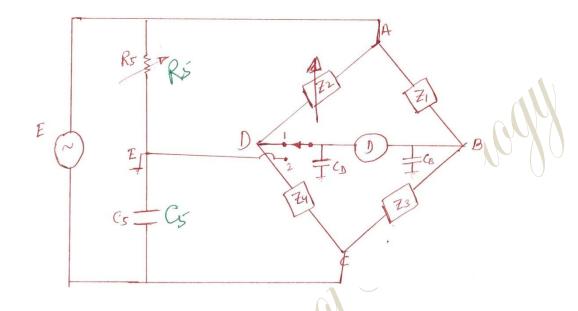
$$2.5.2 \text{ High Voltage ScheringBridge}$$

Fig 2.25 High Voltage Schering bridge

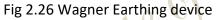
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(1) The high voltage supply is obtained from a transformer usually at 50HZ.



2.6 Wagner earthingdevice:



Wagner earthing consists of 'R' and 'C' in series. The stray capacitance at node 'B' and 'D' are C_B , C_D respectively. These Stray capacitances produced error in the measurements of 'L' and 'C'. These error will predominant at high frequency. The error due to this capacitance can be eliminated using wagner earthingarm.

Close the change over switch to the position (1) and obtained balanced. Now change the switch to position (2) and obtained balance. This process has to repeat until balance is achieved in both the position. In this condition the potential difference across each capacitor is zero. Current drawn by this is zero. Therefore they do not have any effect on themeasurements.

What are the sources of error in the bridge measurements?

- ✓ Error due to stray capacitance and inductance.
- ✓ Due to externalfield.
- ✓ Leakage error: poor insulation between various parts of bridge can produced thiserror.
- ✓ Eddy currenterror.
- ✓ Frequencyerror.

- ✓ Waveform error (due toharmonics)
- ✓ Residual error: small inductance and small capacitance of the resistor produce thiserror.

Precaution

- ✓ The load inductance is eliminated by twisting the connecting the connectinglead.
- ✓ In the case of capacitive bridge, the connecting lead are kept apart. (:: $C = \frac{A \in 0 \in r}{C}$)
- ✓ In the case of inductive bridge, the various arm are magneticallyscreen.
- In the case of capacitive bridge, the various arm are electro statically screen to reduced the stray capacitance between variousarm.
- ✓ To avoid the problem of spike, an inter bridge transformer is used in between the source andbridge.
- The stray capacitance between the ends of detector to the ground, cause difficulty in balancing as well as error in measurements. To avoid this problem, we use wagner earthingdevice.

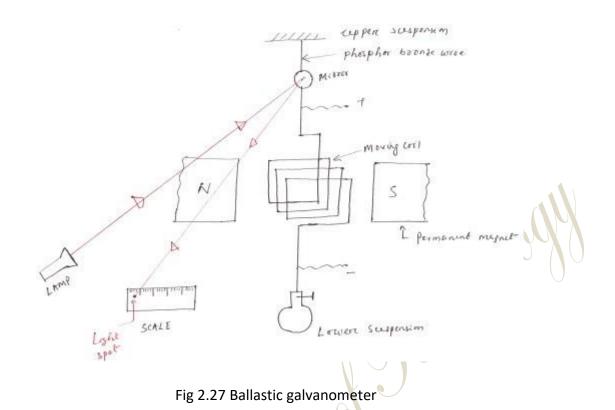
2.7 Ballasticgalvanometer

This is a sophisticated instrument. This works on the principle of PMMC meter. The only difference is the type of suspension is used for this meter. Lamp and glass scale method is used to obtain the deflection. A small mirror is attached to the moving system. Phosphorous bronze wire is used forsuspension.

When the D.C. voltage is applied to the terminals of moving coil, current flows through it. When a current carrying coil kept in the magnetic field, produced by permanent magnet, it experiences a force. The coil deflects and mirror deflects. The light spot on the glass scale also move. This deflection is proportional to the current through thecoil.

$$i=\frac{Q}{t}, Q=it=jidt$$

 $\theta \propto Q$, deflection \propto Charge



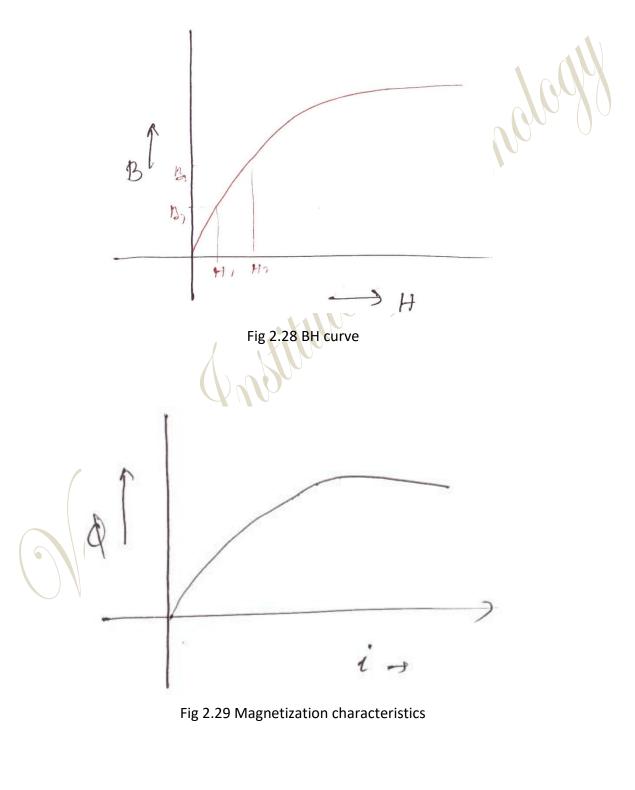
2.8 Measurements of flux and flux density (Method ofreversal)

D.C. voltage is applied to the electromagnet through a variable resistance R_1 and a reversing switch. The voltage applied to the toroid can be reversed by changing the switch from position 2 to position '1'. Let the switch be in position '2' initially. A constant current flows through the toroid and a constant flux is established in the core of the magnet.

A search coil of few turns is provided on the toroid. The B.G. is connected to the search coil through a current limiting resistance. When it is required to measure the flux, the switch is changed from position '2' to position '1'. Hence the flux reduced to zero and it starts increasing in the reverse direction. The flux goes from $+ \phi$ to $- \phi$, in time 't' second. An emf is induced in thesearchcoil,sciencethefluxchangeswithtime.ThisemfcirculatesacurrentthroughR₂and B.G. The meter deflects. The switch is normally closed. It is opened when it is required to take the reading.

2.8.1 Plotting the BHcurve

The curve drawn with the current on the X-axis and the flux on the Y-axis, is called magnetization characteristics. The shape of B-H curve is similar to shape of magnetization characteristics. The residual magnetism present in the specimen can be removed as follows.



Close the switch S_2' to protect the galvanometer, from high current. Change the switch S1 from position '1' to '2' and vice versa for several times.

To start with the resistance ' R_1 ' is kept at maximum resistance position. For a particular value of current, the deflection of B.G. is noted. This process is repeated for various value of current. For

each deflection flux can be $B = \frac{\phi}{A}$) calculated.(

Magnetic field intensity value for various current can be calculated.().The B-H curve can be plotted by using the value of 'B' and 'H'.

2.8.2 Measurements of iron loss:

Let R_P= pressure coil resistance

R_s = resistance of coilS1

E= voltage reading= Voltage induced in S₂

I= current in the pressure coil

V_P= Voltage applied to wattmeter pressure coil.

W= reading of wattmeter corresponding voltage V

W₁= reading of wattmeter corresponding voltage

$$W \rightarrow V \qquad \qquad W_1 = \stackrel{E}{\Longrightarrow} W$$

 $W_1 \rightarrow E_P \qquad W \qquad V \qquad ^1 \qquad V$

W1=Total loss=Iron loss+ Cupper loss.

The above circuit is similar to no load test of transformer.

In the case of no load test the reading of wattmeter is approximately equal to iron loss. Iron loss depends on the emf induced in the winding. Science emf is directly proportional to flux. The voltage applied to the pressure coil is V. The corresponding of wattmeter is 'W'. The iron loss

corresponding E is $E = \frac{WE}{V}$. The reading of the wattmeter includes the losses in the pressure coil and copper loss of the winding S1. These loses have to be subtracted to get the actual iron loss.

2.9 Galvanometers

D-Arsonval Galvanometer

Vibration Galvanometer

Ballistic C

2.9.1 D-arsonval galvanometer (d.c.galvanometer)

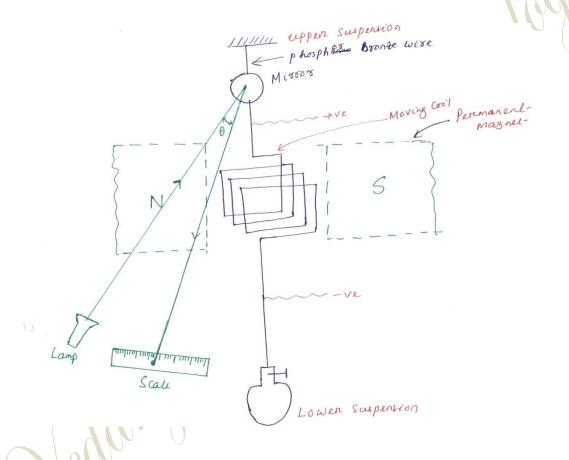


Fig 2.30 D-Arsonval Galvanometer

Galvanometer is a special type of ammeter used for measuring A or mA. This is a sophisticated instruments. This works on the principle of PMMC meter. The only difference is thetypeofsuspensionusedforthismeter. It uses a sophisticated suspension called taut suspension, so that moving system has negligible weight.

Lamp and glass scale method is used to obtain the deflection. A small mirror is attached to the moving system. Phosphors bronze is used forsuspension.

When D.C. voltage is applied to the terminal of moving coil, current flows through it. When current carrying coil is kept in the magnetic field produced by P.M., it experiences a force. The light spot on the glass scale also move. This deflection is proportional to the current through the coil. This instrument can be used only with D.C. like PMMCmeter.

huger

The deflecting Torque,

T_D=BINA T_D=GI, Where G=BAN T_C=K_S*θ*=S*θ*

At balance, $T_C=T_D \Longrightarrow S \theta = GI$

∴*θ*=^{GI}___

Where G= Displacements constant of Galvanometer S=Spring constant

2.9.2 Vibration Galvanometer (A.C. Galvanometer)

The construction of this galvanometer is similar to the PMMC instrument except for the moving system. The moving coil is suspended using two ivory bridge pieces. The tension of the system can be varied by rotating the screw provided at the top suspension. The natural frequency can be varied by varying the tension wire of the screw or varying the distance between ivory bridge piece.

When A.C. current is passed through coil an alternating torque or vibration is produced. This vibration is maximum if the natural frequency of moving system coincide with supply frequency. Vibration is maximum, science resonance takes place. When the coil is vibrating, the mirror oscillates and the dot moves back and front. This appears as a line on the glass scale. Vibration galvanometer is used for null deflection of a dot appears on the scale. If the bridge is unbalanced, a line appears on the scale

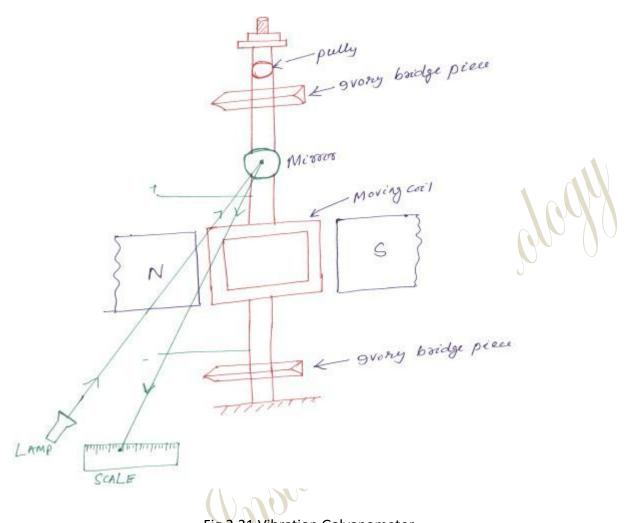


Fig 2.31 Vibration Galvanometer

Example 2.2-In a low- Voltage Schering bridge designed for the measurement of permittivity, the branch 'ab' consists of two electrodes between which the specimen under test may be inserted, arm 'bc' is a non-reactive resistor R_3 in parallel with a standard capacitor C_3 , arm CD is a non-reactive resistor R_4 in parallel with a standard capacitor C_4 , arm 'da' is a standard air capacitor of capacitance C_2 . Without the specimen between the electrode, balance is obtained with following values , $C_3=C_4=120$ pF, $C_2=150$ pF, $R_3=R_4=5000\Omega$. With the specimen inserted, these values become $C_3=200$ pF, $C_4=1000$ pF, $C_2=900$ pF and $R_3=R_4=5000\Omega$. In such test w=5000 rad/sec. Find the relative permittivity of thespecimen?

Sol:Relative permittivity(\mathcal{E}_r) = $\frac{\text{capacitance measured with given medium}}{\text{capacitance measured with air medium}}$

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Fig 2.32 Schering bridge

Rs

echnolo

$$C_1 = C_2 (\frac{R_4}{R_3})$$

Let capacitance value C₀, when without specimen dielectric.

Cr

Let the capacitance value C_s when with the specimendielectric.

$$C = C \begin{pmatrix} R_{4} \\ 2 \\ R_{3} \end{pmatrix} = 150 \times \frac{5000}{5000} = 150 \ pF$$

$$C_{s} = C_{2} \begin{pmatrix} R_{4} \\ R_{3} \end{pmatrix} = 900 \times \frac{5000}{5000} = 900 \ pF$$

$$\mathcal{E} = \frac{C_{s}}{r} = \frac{900}{150} = 6$$

Example 2.3- A specimen of iron stamping weighting 10 kg and having a area of 16.8 cm² is tested by an episten square. Each of the two winding S₁ and S₂ have 515 turns. A.C. voltage of 50 HZ frequency is given to the primary. The current in the primary is 0.35 A. A voltmeter connected to S₂ indicates 250 V. Resistance of S₁ and S₂ each equal to 40 Ω . Resistance of pressure coil is 80 k Ω . Calculate maximum flux density in the specimen and iron loss/kg if the wattmeter

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indicates 80 watt?

Sol^a-
$$E = 4.44 f \phi_m N$$

 $B_m = \frac{E}{4.44 f AN}$
Iron loss= $W (1 + \frac{R_5}{R_p}) - \frac{E^2}{(R_5 + R_p)}$
 $= 80(1 + \frac{40}{80 \times 10^3}) - \frac{250^2}{(40 + 80 \times 10^3)} = 79.26 watt$

Iron loss/ kg=79.26/10=7.926 w/kg

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